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18. Simulation of tracked vehicle dynamics

UM Tracked Vehicle module has been developed for an automatic generation of models of tracked vehicles (TV) and analysis of their dynamics.

In the current UM version, the following tools are available in UM Tracked Vehicle:

- Automatic generation of tracks with the help of library of basic track components.
- Expansion of the library by the user’s components.
- Dynamic analysis of tracked vehicle using standard dynamic tests.

To verify, whether the current UM version includes the module of simulation of TV, run the UM Input program and call the About window by the Help | About… menu command. The module UM Tracked Vehicle is available if it is marked by the (+) sign, Figure 18.1.

Standard model of a TV includes (Figure 18.2)

- hull,
- two tracks,
- elements of transmission,
additional mechanisms tools and manipulators, if necessary.

Development of a track model is automated to a considerable degree. If necessary, a detailed modeling a transmission by the user is possible with standard UM elements.

In the current UM version, several types of TV suspensions can be modeled: fixed, bogies, torsion-bar suspension etc.

We recommend to start studying the UM Tracked Vehicle module with the file gs_UM_Caterpillar.pdf.

It is recommended also to look at TV models, which are included in UM Tracked Vehicle standard configuration:

{UM Data}\SAMPLES\Tracked_Vehicles\gsTV;
{UM Data}\SAMPLES\Tracked_Vehicles\M1A1;
{UM Data}\SAMPLES\Tracked_Vehicles\FH200.
Chapter 18. Tracked vehicles

18.1. Development of TV models in UM Input program

18.1.1. Standard elements of tracked suspension

18.1.1.1. Specification of elements and their models

An example of tracked suspension (a torsion bar suspension) is shown in Figure 18.3. The main elements of the track model are:

- suspension with *road wheels*;
- *sprocket*;
- *track chain* consisting of a number of rigid *track links*, connected by *rigid, flexible or parallel* joints;
- *idler* with a tension mechanism;
- *rollers*.

To automate the process of development of a track model, a set of standard or user’s created components are used, as well as a special tool for description of a track in the Input module.

The standard components are located in text files in the directory `{UM Data}\Caterpillar\Subsystems`.

Here is the list of the standard components.

1. **Suspensions**:
   - `torsion_bar_wheel.dat` is a unit of the torsion bar suspension, which includes one road wheel and torsion bar;
   - `bogie_joint.dat` is a suspension bogie with two road wheels connected to the hull by a revolute joint;
   - `bogie_torsion.dat` is a suspension bogie with two road wheels connected to the hull by a torsion bar.

2. **Sprocket**: `sprocket.dat`.

![Figure 18.3. Example of a tracked suspension](attachment:image.png)
3. **Idler with a tension device:**
   - `idler_crank_simple.dat` is a simplified model of an idler on a crank;
   - `idler_crank.dat` is a more detailed model of an idler on a crank;
   - `idler_slider.dat` is a model of an idler on a slider.

4. **A track link**
   - `track_link_rigid.dat` is a track link with a rigid joint;
   - `track_link_bushing.dat` is a track link with a flexible joint (bushing);
   - `track_link_parallel.dat` is a track with two flexible (parallel) joints (bushings).

5. **A roller:** `roller.dat`.

Using the components as well as geometric data, UM automatically generates track models.
18.1.1.2. Main system of coordinates

The standard system of coordinates in UM Tracked Vehicle coincides with inertial frame SC0. Their axes have the following directions:

- X-axis is directed forward along the axis of symmetry of TV in its initial position;
- Z-axis is directed vertically upward;
- Y-axis is directed to the left from the forward motion.

As a rule, the rotation axis of a sprocket (rear drive TV) or an idler (front drive TV) is located in YZ plane of SC0 with zero value of longitudinal coordinate, Figure 18.3, so that X coordinates of other wheels and rollers are positive.

18.1.1.3. Local systems of coordinates for wheels and rollers

![Figure 18.4. LSC for road wheel](image)

Local systems of coordinates (LSC) for bodies, which model road wheels, idler, sprocket and rollers, meet some requirement. Origins of this SC must be located in the centers of the wheels, Figure 18.4. In particular, rotation axis of wheels must pass through the origins of LSC. All standard components satisfy this claim. The user should remember it when developing its own components, Section 18.1.3 *Registration of new TV components*. 
18.1.1.4. Description of standard components

18.1.1.4.1. Suspension

Elements of suspension are developed as included subsystems.

![Image of suspension systems](image)

Figure 18.5. Examples of subsystems describing elements of suspension. Torsion bar and joint bogie suspensions

Each unit of the subsystem contains one (individual suspensions) or several (bogies) road wheels, Figure 18.5.

*If necessary, a subsystem might contain a full description of track suspension and all road wheels.*
18.1.1.4.1.1. Standard elements and identifiers of suspension subsystems

A correct description of suspension unit requires use of standard elements.

A local hull is a massless body with 6 degrees of freedom (d.o.f.) marked with the text attribute of C-type: LocalHull, Figure 18.6.

Remark. There exist in UM two types of text attributes, which are used for internal identification of some elements, in particular, bodies. They are named attributes of C-type and T-type. The attribute of C-type can be assigned in the Comments/Text attribute C box, Figure 18.6. Both attributes are available on the Object | Attributes tab of the inspector, Figure 18.7.

The body Local hull is used by description of joints and force elements connecting bodies of the suspension with the hull of TV. The hull is not included in the suspension unit, and joints and force elements are connected with the local hull. By automatic development of a track model, the local hull of the subsystem unit is rigidly connected by UM with the analogous local hull of the
track, and the internal joint with 6 d.o.f. is ignored. After that the local hull of the track is rigidly connected with the hull of TV, and, in fact, elements of suspension are attached to the real hull of TV.

While creating a body *Local hull*, the button must be used to generate a body with an internal joint, Figure 18.6.

Figure 18.8. Text attributes on the Bodies and Object | Attributes | Bodies tabs

Standard element: text attribute of a road wheel *RoadWheel*.

Bodies modeling road wheels must be marked by the text attribute of C-type *RoadWheel*, Figure 18.8.

Standard elements: standard identifiers, Table 18.1, Figure 18.9.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>xbogie</em></td>
<td>Position of subsystem relative to SC0 in longitudinal direction</td>
</tr>
<tr>
<td><em>rroadwheel</em></td>
<td>Radius of road wheel</td>
</tr>
<tr>
<td><em>wroadwheel</em></td>
<td>Width of road wheel</td>
</tr>
<tr>
<td><em>side_key</em></td>
<td>Indicator of a left (1) or right (-1) track. This identifier should be used for specifying lateral coordinates, which have different signs for the left and right tracks</td>
</tr>
<tr>
<td><em>wguide</em></td>
<td>Width of a slot in the wheel for run of track teeth</td>
</tr>
<tr>
<td><em>hguide</em></td>
<td>Depth of a slot in the wheel for run of track teeth</td>
</tr>
<tr>
<td><em>guide_in_key</em></td>
<td>Indicator of existence (1) or absence (0) of the slot for run of track teeth</td>
</tr>
</tbody>
</table>
Remark. Geometrically, models of suspension units are developed in such a way that by 
side_key=1 the geometry corresponds to the left track, whereas by side_key=1 to 
the right one. With this purpose, the identifier is used as a multiplier for geomet- 
rical parameters having different signs for the left and right tracks. 
Example: -y_road_arm_joint*side_key
18.1.1.4.1.2. Selected identifiers of suspension subsystems

To get access to the most important geometrical parameters of suspension unit by generation of a track, it is recommended to create a list of selected identifiers, which parameterize necessary parameters in the suspension. List of selected identifiers denotes a set of identifiers of the owner object (an object that owns the subsystem), which names coincide with the names of corresponding identifiers of the subsystem.

Models of the standard suspension units contain ready lists of selected identifiers, which can be modified by the user.

To create and modify the list of selected identifiers, the following steps are necessary.
1. Create a new object in **UM Input**.
2. Read a component by the button or by the **Edit | Read from file...** menu command.

![Figure 18.10. Adding selected identifiers from subsystem](image)

3. To add new identifiers to the list of selected identifiers, click the right mouse button on the list and then click the **Add from subsystems** menu item (Figure 18.10, left).
4. Add necessary identifiers by clicking on the corresponding elements of the appeared list, Figure 18.10, right.
5. Save the modified component by the button on the tool panel or by the **File | Save as component...** menu command.
Figure 18.11. List of selected identifiers of torsion bar suspension in the wizard of track

After adding a suspension unit to the track model, the selected identifiers become available for modification their numeric values on the **Identifiers | Suspension** tab, Figure 18.11.
### 18.1.1.4.1.3. Torsion bar suspension

This suspension unit models the most frequently used torsion bar suspension.

1. **Path to the component file:** `{UM Data}\Caterpillar\Subsystems\torsion_bar_wheel.dat`.
2. **Selected identifiers**, Table 18.2, Figure 18.12.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>l_road_arm</td>
<td>0.5</td>
<td>(m) length of torsion arm</td>
</tr>
<tr>
<td>alpha_stat</td>
<td>20</td>
<td>(degrees) Angle of the arm inclination to the horizon by static position of TV</td>
</tr>
<tr>
<td>f_stat</td>
<td>70</td>
<td>(mm) Static vertical travel of wheel</td>
</tr>
<tr>
<td>f_dyn</td>
<td>120</td>
<td>(mm) Maximal dynamic vertical travel of wheel</td>
</tr>
<tr>
<td>p_stat</td>
<td>7000</td>
<td>(N) Static load for a wheel</td>
</tr>
<tr>
<td>rear_arm</td>
<td>1</td>
<td>(±1) Key for direction of the torsion axis relative to the wheel: rear (1) or front (-1)</td>
</tr>
</tbody>
</table>

Figure 18.12. Torsion bar suspension and selected identifiers

Figure 18.13. Change of the torsion arm orientation using the rear_arm identifier value
Specifying different values if the \textit{rear\_arm} identifiers for subsystems, the user can get geometrically different orientations of torsion arms in the track model, Figure 18.13. In this example, the value -1 is set for all suspension subsystems whereas the value +1 is set for the first one.

Angles $\alpha_u, \alpha_d$ and torsion stiffness are computed automatically according to the formulas

$$
\alpha_u = \arcsin \left( \frac{f_{\text{dyn}}}{l_{\text{road\_arm}}} - \sin(\alpha_{\text{stat}}) \right) + \alpha_{\text{stat}}
$$

$$
\alpha_d = \arcsin \left( \frac{f_{\text{stat}}}{l_{\text{road\_arm}}} + \sin(\alpha_{\text{stat}}) \right) - \alpha_{\text{stat}}
$$

$$
c = \frac{p_{\text{stat}} \cdot l_{\text{road\_arm}} \cdot \cos(\alpha_{\text{stat}})}{\alpha_d}
$$

3. **Bodies.**

The model includes three bodies.

- Road wheel, marked by the standard text attribute of C-type: \texttt{RoadWheel}.
- Torsion arm \texttt{RoadArm}.

Inertia parameters are presented in Table 18.3.

<table>
<thead>
<tr>
<th>Body</th>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Road Wheel</strong></td>
<td>$m_{\text{road_wheel}}$</td>
<td>100 (kg) Mass</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$ix_{\text{road_wheel}}$</td>
<td>10 (kg m$^2$) Moment of inertia relative to the axis in the wheel plane</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$iy_{\text{road_wheel}}$</td>
<td>20 (kg m$^2$) Moment of inertia relative to the wheel symmetry axis</td>
<td></td>
</tr>
<tr>
<td><strong>Road Arm</strong></td>
<td>$m_{\text{road_arm}}$</td>
<td>50 (kg) Mass</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$ix_{\text{road_arm}}$</td>
<td>0.2 (kg m$^2$) Moment of inertia relative to the arm axis</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$iy_{\text{road_arm}}$</td>
<td>3 (kg m$^2$) Moment of inertia relative to the axis perpendicular to the arm</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$iz_{\text{road_arm}}$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
4. **Joints.**

Besides the internal joint of local hull, the model contains two rotational joints, Figure 18.14.

- The *jRoad arm* joint introduces a rotational degree of freedom of the torsion arm relative to the hull. In the subsystem, this joint specifies the rotation of arm (body *Road arm*) relative to the local hull (body *Local hull*). The joint is of the *generalized type* and contains three elementary transformations (ET). Consider ET in more details.

As it is known, a joint of the generalized type is described by a sequence of ET, which transforms SC of the first body to SC of the second one, Figure 18.15, [Chapter 2, Sect. Joints | Generalized joint.](#)
Chapter 18. Tracked vehicles

Figure 18.16. First ET: translation

The first ET of the tc type shifts the origin of the SC of the local hull into the joint point, which lies on the joint axis. The result of this shift is shown in Figure 18.16 by thin lines:

- shift along the X-axis is set by the expression

\[ l_{road\_arm}\cos(\alpha_{stat}\,dtor)+xbogie, \]

where \( xbogie \) is the position of wheel center relative to SC0 in X-direction; the standard identifier \( drot (=\pi/180) \) transforms degrees to radians;

- shift along the Y-axis

\[ -y_{road\_arm\_joint}\times side\_key, \]

please note that the direction of shift depends on the value of identifier \( side\_key \) (±1);

- shift along the Z-axis:

\[ rroadwheel+l_{road\_arm}\sin(\alpha_{stat}\,dtor). \]

Figure 18.17. Second ET: parameterized rotation
The second ET of the tt type makes rotation on the alpha_stat angle about the joint axis, Figure 18.17.

Figure 18.17. Third ET: introduction of rotational degree of freedom and joint torque

The third ET of the tv type introduces a rotational degree of freedom and the torsional spring as a joint torque, Figure 18.18.

The positive direction corresponding to decrease of the joint coordinate is shown in Figure 18.19 for different orientations of the torsion arm (identifier rear_arm=±1).

Figure 18.19. Direction of positive rotation in joint

Parameters of torsion spring.
The linear torsion bar suspension is implemented in the model, Figure 18.18. By zero joint coordinate, the torque in joint is equal to the parameterized value preload. Direction of this torque for different orientation of the arm is shown in Figure 18.20. Torsion spring parameters are set by identifiers c_torsion (stiffness constant) and d_torsion (damping constant).
The second nonlinear component of the joint torque realizes the limitation of upward travel $f_{dyn}$ of the road wheel. By exceeding the travel value, a restoring torque with the parameterized stiffness $c_{stop}$ appears, Figure 18.21, Figure 18.22, Table 18.4.

![Figure 18.20. Static torques](image)

![Figure 18.21. Limitation of vertical travel](image)
rear_arm=-1

rear_arm=+1

Figure 18.22. Nonlinear limitation torque for different orientation of torsion arm

Table 18.4

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>preload</td>
<td>-</td>
<td>(Nm) Static torque</td>
</tr>
<tr>
<td>c_torsion</td>
<td>-</td>
<td>(Nm/rad) Torsion stiffness of suspension</td>
</tr>
<tr>
<td>d_torsion</td>
<td>100</td>
<td>(Nms/rad) Torsion damping</td>
</tr>
<tr>
<td>c_stop</td>
<td>10 000 000</td>
<td>(Nm/rad) Torsion stiffness of wheel stop</td>
</tr>
</tbody>
</table>

Remark. Static torque can be computed according to the following approximate formula:
\[
\text{preload} \approx \frac{Mgl \cos \alpha_0}{2n}.
\]

Here \( M \) is the sprung mass of TV, \( g \) is the gravity acceleration, \( l \) is the arm length, \( \alpha_0 = \alpha_{\text{stat}} \), \( n \) is the number of road wheels.

- The \( j\text{Road} \) wheel joint specifies a rotational degree of freedom of the road wheel relative to the arm. The lateral coordinate of the joint point is set by the expression
  \[-y_{\text{road_arm_joint}} \times \text{side_key}.
\]
  Due to the \( \text{side_key} \) identifier, this coordinate changes its sign for the left and right tracks.

5. **Images.**
   - The graphic object \( \text{Road wheel} \) is assigned to the body of the same name.

![Figure 18.23. Arm image by side_key=±1](image)

![Figure 18.24. Parameterization of graphic element rotation by the identifier side_key=±1](image)

- The \( \text{Road arm} \) graphic object is assigned to the body of the same name. This graphic object must be specular reflected for the left and right tracks, Figure 18.23. To implement the reflection, parameterized rotations about the X-axis are made for two cylinders, Figure 18.24.
18.1.1.4.1.4. Suspension bogie with two wheels and two arms

This unit models a suspension bogie with two road wheels and two arms connected by a rotational joint A, Figure 18.25, Figure 18.26. The front arm is connected with the hull by a rotational joint B. A spring connects both arms.
Figure 18.26. Selected identifiers

1. **Path to the component file**: `{UM Data}\Caterpillar\Subsystems\bogie_2arm.dat`.

2. **Selected identifiers**, Figure 18.26, Table 18.5.

**Table 18.5**

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>wheel_base</td>
<td>0.5</td>
<td>(m) Distance between wheel centers</td>
</tr>
<tr>
<td>x_spring_front</td>
<td>0.1</td>
<td>(m) X position of front spring end relative to the center of the front wheel (positive backward)</td>
</tr>
<tr>
<td>x_spring_rear</td>
<td>0.1</td>
<td>(m) X position of rear spring end relative to the center of the rear wheel (positive forward)</td>
</tr>
<tr>
<td>x_arm_joint</td>
<td>0.19</td>
<td>(m) X, Z coordinates of joint A relative to the center of rear wheel</td>
</tr>
<tr>
<td>z_arm_joint</td>
<td>0.15</td>
<td></td>
</tr>
<tr>
<td>x_bogie_joint</td>
<td>0.21</td>
<td>(m) X, Z coordinates of joint B relative to the center of front wheel</td>
</tr>
<tr>
<td>z_bogie_joint</td>
<td>0.13</td>
<td></td>
</tr>
</tbody>
</table>

3. **Bodies.**

   The model includes five bodies.
- Local hull, see Sect. 18.1.1.4.1.1. "Standard elements and identifiers of suspension subsystems", p. 18-10.
- Road wheel front, Road wheel rear marked by the standard text attribute of C-type: RoadWheel.
- Road arm front, Road arm rear.
  Inertia parameters are listed in Table 18.6.

### Table 18.6

<table>
<thead>
<tr>
<th>Body</th>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Road wheel front (rear)</td>
<td>m_road_wheel</td>
<td>100</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_road_wheel</td>
<td>5</td>
<td>(kg m²) Moment of inertia relative to the axis in the wheel plane</td>
</tr>
<tr>
<td></td>
<td>iy_road_wheel</td>
<td>10</td>
<td>(kg m²) Moment of inertia relative to the rotation axis</td>
</tr>
<tr>
<td>Road Arm front (rear)</td>
<td>m_road_arm</td>
<td>10</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_road_arm</td>
<td>1</td>
<td>(kg m²) Moment of inertia relative to the central axes</td>
</tr>
<tr>
<td></td>
<td>iy_road_arm</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td></td>
<td>iz_road_arm</td>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

**Figure 18.27. Joint of bogie with two arms**

4. **Joints.**

Besides the internal joint of the local hull, the model of the suspension unit includes four rotational joints, Figure 18.27:
- joints connecting road wheels with arms (jRoad wheel rear, jRoad wheel front);
- joint jRoad arm connecting two arms (A in Figure 18.26);
- joint jBogie connecting the front arm with the local hull (B in Figure 18.26).

**Suspension parameters.**
In the model, a linear suspension is implemented by the bipolar force element \textit{Spring}. Type of force element: \textit{Linear}, Figure 18.28. The force element is described by two main parameters: the preliminary load \textit{Preload} and the spring constant \textit{c\_spring}.

The preload compensates the static load.

Using the equilibrium equations as well as the scheme in Figure 18.29, it is easy to get the spring preload value \( P \) by the load value \( F \) in joint B.

\[
P = F \left( \frac{x_A x_B}{b(z_s - z_A)} \right)
\]
18.1.1.4.1.5. Torsion two-wheeled bogie

Figure 18.30. Bogie with the torsion-bar (left); selected identifiers (right)

The unit models a bogie with two road wheels and a torsion bar, Figure 18.30. The torsion bar can be replaced by a cylindrical spring connecting the arm with the hull.

1. **Path to the component file:**
   
   `{UM Data}\Caterpillar\Subsystems\bogie_2wheel_1arm.dat`.

2. **Selected identifiers**, Table 18.7, Figure 18.30.

### Table 18.7

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>wheel_base</td>
<td>0.5</td>
<td>(m) distance between the wheels</td>
</tr>
<tr>
<td>l_road_arm</td>
<td>0.5</td>
<td>(m) Length of arm</td>
</tr>
<tr>
<td>ra_angle</td>
<td>30</td>
<td>(degrees) Static angle of arm to the horizontal axis</td>
</tr>
<tr>
<td>z_arm_joint</td>
<td>0.1</td>
<td>(m) Vertical position of bogie joint relative to the wheel centers</td>
</tr>
<tr>
<td>dx_arm_joint</td>
<td>0</td>
<td>(m) Longitudinal shift of the arm joint</td>
</tr>
</tbody>
</table>

Figure 18.31. Change of the arm orientation by the static angle
Setting different values of the ra_angle value, the user can get various orientations of the arm, Figure 18.31.

3. **Bodies.**

The model contains four bodies.
- Local hull, Sect. 18.1.1.4.1.1. "Standard elements and identifiers of suspension subsy-
  systems", p. 18-10.
- Two wheels (Road wheel front, Road wheel rear), marked by the standard text attribute of C-type: RoadWheel.
- Bogie frame.
- Road Arm.

Inertia parameters are specified in Table 18.8.

<table>
<thead>
<tr>
<th>Body</th>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Road Wheel</strong></td>
<td>m_road_wheel</td>
<td>100</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_road_wheel</td>
<td>10</td>
<td>(kg m²) Moment of inertia relative to the axis in the wheel plane</td>
</tr>
<tr>
<td></td>
<td>iy_road_wheel</td>
<td>20</td>
<td>(kg m²) Moment of inertia relative to the axis perpendicular to the wheel plane</td>
</tr>
<tr>
<td><strong>Bogie frame</strong></td>
<td>m_frame</td>
<td>50</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_frame</td>
<td>3</td>
<td>(kg m²) Frame moments of inertia</td>
</tr>
<tr>
<td></td>
<td>iy_frame</td>
<td>10</td>
<td></td>
</tr>
<tr>
<td></td>
<td>iz_frame</td>
<td>10</td>
<td></td>
</tr>
<tr>
<td><strong>Road Arm</strong></td>
<td>m_road_arm</td>
<td>50</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_road_arm</td>
<td>0.2</td>
<td>(kg m²) Moment of inertia relative to the arm axis</td>
</tr>
<tr>
<td></td>
<td>iy_road_arm</td>
<td>3</td>
<td>(kg m²) Moments of inertia perpendicular to the arm axis</td>
</tr>
<tr>
<td></td>
<td>iz_road_arm</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 18.8

Inertia parameters

Figure 18.32. Joints
4. **Joints.**

Four rotational joints are shown in Figure 18.32, see Sect. 18.1.1.4.1.4. "Suspension bogie with two wheels and two arms", p. 18-23.

5. **Suspension parameters.**

A linear torsion spring is implemented in the model.
18.1.1.4.1.6. Road wheel for fixed suspension

This model contains one wheel with rotational degree of freedom relative to the local hull. In case of a fixed suspension, the local hull is rigidly connected with the TV hull.

1. Path to the component file: `{UM Data}\Caterpillar\Subsystems\Single_wheel.dat`.
2. Selected identifiers are not used.
3. Bodies.
   - Road wheel marked by the standard text attribute of C-type: RoadWheel.
   Inertia parameters are presented in Table 18.9.

<table>
<thead>
<tr>
<th>Body</th>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Road Wheel</td>
<td>$m_{road_wheel}$</td>
<td>100</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>$ix_{road_wheel}$</td>
<td>10</td>
<td>(kg m$^2$) Moment of inertia relative to the axis in the wheel plane</td>
</tr>
<tr>
<td></td>
<td>$iy_{road_wheel}$</td>
<td>20</td>
<td>(kg m$^2$) Moment of inertia relative to the axis perpendicular to the wheel plane</td>
</tr>
</tbody>
</table>

   One rotation joint connects the road wheel with the local hull.
18.1.1.4.2. Idler and tension device

As the standard models of the idler with tension devise, three components are delivered with UM, which differ in the tension mechanism design:
- `idler_crank_simple` is a simplified model of the idler on a crank, Figure 18.34, left;
- `idler_crank` is a more detailed model of the idler on a crank, Figure 18.34, center;
- `idler_slider` is the model of the idler on a slider, Figure 18.34, right.

Standard elements
1. **Standard identifiers:** any component describing the idler must contain standard identifiers, Table 18.10, Figure 18.48.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>ridler</td>
<td>(m) Radius of idles</td>
</tr>
<tr>
<td>widler</td>
<td>(m) Width of idler</td>
</tr>
<tr>
<td>side_key</td>
<td>Key: left (1) or right (-1) track. The identifier should be used as a factor by lateral geometrical parameters, which have different signs for the left and right tracks</td>
</tr>
<tr>
<td>wguide</td>
<td>Width of a slot in the wheel for run of track teeth</td>
</tr>
<tr>
<td>hguide</td>
<td>Depth of a slot in the wheel for run of track teeth</td>
</tr>
<tr>
<td>xcidler</td>
<td>X coordinate of idler axis</td>
</tr>
<tr>
<td>zcidler</td>
<td>Z coordinate of idler axis</td>
</tr>
<tr>
<td>rear_drive_key</td>
<td>Key for position of drive wheel: 1 (rear), -1 (front)</td>
</tr>
</tbody>
</table>

2. **Standard element:** a text attribute for idler identification. An idler body must be marked by a standard text attribute of C-type: `Idler`, Figure 18.35.

3. **Description of elements connected with the TV hull.**

   In opposite to the suspension components, description of the idler does not include a subsystem and a local hull. All elements connected with the TV hull, are coupled with `Base0`. By including a component in the model of a track, the base body is replaced automatically by the track local hull.
The idler components are similar, and we consider the first of them in a little bit more details.
18.1.4.2.1. Idler on a crank. A simplified model

Consider a simplified model of an idler with a crank, Figure 18.36. The name of the component is *idler_crank_simple*. Simplification of the component in comparison with the more detailed one (*idler_crank*) consists in reduction of force parameters to the rotational joint connecting the idler and the TV hull.

The model contains the idler and crank connected by a rotational joint, as well as a joint connecting the idler with the hull.

1. **Path to the component file:**
   {UM Data}\Caterpillar\Subsystems\idler_crank_simple.dat

2. **Identifiers.** In addition to identifiers listed in Table 18.10, a number of identifiers are used for description of geometric parameters of the model, Table 18.11, Figure 18.36.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$l_{\text{crank}}$</td>
<td>(m) Length of crank is the distance between the rotational joints</td>
</tr>
<tr>
<td>$\text{crank_angle_0}$</td>
<td>(Degrees) Angle $\alpha$ is the nominal orientation of the crank. Direction of the rotation depends on the identifier rear_drive_key. Positive direction for rear_drive_key=1 is shown in Fig-</td>
</tr>
</tbody>
</table>
3. **Bodies.**

The model contains two bodies.

- *Idler* body marked by the standard text attribute of C-type: *Idler*.
- *Tension crank*.

Inertia parameters are listed in Table 18.12.

<table>
<thead>
<tr>
<th>Body</th>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Idler</td>
<td>m_idler</td>
<td>100</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_idler</td>
<td>7</td>
<td>(kg m$^2$) Moment of inertia relative to the axis in the wheel plane</td>
</tr>
<tr>
<td></td>
<td>iy_idler</td>
<td>15</td>
<td>(kg m$^2$) Moment of inertia relative to the axis perpendicular to the wheel plane</td>
</tr>
<tr>
<td>Tension crank</td>
<td>m_crank</td>
<td>10</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td></td>
<td>ix_crank</td>
<td>1</td>
<td>(kg m$^2$) Moment of inertia of the crank</td>
</tr>
<tr>
<td></td>
<td>iy_crank</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>iz_crank</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

4. **Joints.**

The model contains two rotational joints, Figure 18.37.
The $jTension$ crank joint introduces a rotational degree of freedom of the crank relative to the hull. In the component model, this joint connects the crank with Base0. The joint is of the generalized type and includes four elementary transformations (ET). Consider ET in more details.

As it is known, the generalized joint specifies a sequence of ET, which transforms system of coordinates of the first body to that of the second one, Figure 18.15, Chapter 2, Sect. Joints | Generalized joint.

**The first ET** of the $tc$ type shifts the origin of SC of the first body into the joint point lying on the axis of rotation. The result is show in Figure 18.39 by thin lines:

- shift along the X-axis is set by the expression
  \[ x_{cidler} + l_{crank} \times sa \times rear\_drive\_key \]

where the $x_{cidler}$ identifiers corresponds to the position of the idler wheel center in the longitudinal direction, \( sa = \sin(\text{crank\_angle\_0} \times \text{dof}) \);

- shift along the Y-axis
  \[ -y_{crank\_joint} \times \text{side\_key} \].

---

**Figure 18.38. Joint $jTension$ crank and body-fixed SC**

**Figure 18.39. The first ET: translation**
note that the direction of the lateral shift depends on the identifier $\text{side_key}$ ($\pm 1$);
- shift along the Z-axis:

$$
z\text{cidler} + l\_\text{crank} \times \text{ca},
$$

$$
\text{ca} = \cos(\text{crank\_angle\_0} \times \text{dtor})
$$

Figure 18.40. The second ET: rotation on a parameterized angle

*The second ET* of the *tt* type realizes a rotation about the joint axis on the angle, which is parameterized by the identifier $\text{crank\_angle\_0}$ (angle $\alpha$ in Figure 18.36), Figure 18.40.

Figure 18.41. The third ET: rotational degree of freedom

*The third ET* of the *tv* type introduces the rotational degree of freedom, Figure 18.41. In this ET, a joint torque is described corresponding to the realization of the tension mechanism.
The final fourth ET of the tc type transforms the SC to the SC of the crank, Figure 18.42.

Figure 18.43. Joint idler_Tension crank

The rotational joint idler_Tension crank introduces a rotational degree of freedom of the idler relative to the crank, Figure 18.43.

5. Joint torque realizing the tension device

The model of tension mechanism realizes the following properties of the real prototype:
- preliminary load of tension spring (identifier pretension);
- linear stiffness of tension spring by compression forces exceeding the preload force (identifier c_tension_spring);
- blocking properties of the device by stretching;
• possibility of getting a desirable track tension by change of the unloaded length of the tension device; change in length is parameterized by the identifier \textit{dl\_tension\_rod}, and increase of this value leads to the increase of the tension.

In the simplified model considered in the current section, the listed properties are implemented by a nonlinear joint torque with a simplified reduction of tension spring properties to the crank joint:

- \( d\_tension\_angle=dl\_tension\_rod/l\_crank \) is the angular analog of change the spring length;
- \( pretension\_torque=pretension*l\_crank \) is the preload torque;
- \( c\_torsional=c\_tension\_spring*sqr(l\_crank) \) is the torsion stiffness approximating the linear spring stiffness.

![Graph](image1)

\text{rear\_drive\_key=1}

![Graph](image2)

\text{rear\_drive\_key=-1}

Figure 18.44. Force characteristics of joint torque for TV with rear / front drive

dl\_tension\_rod=5 \text{ mm}

The joint torque description includes two components one of which is enabled for a rear drive TV (\textit{rear\_drive\_key}=1), and the second one for the front drive TV (\textit{rear\_drive\_key}=-1), Figure 18.44. The steep part of the plot corresponds to the blocking properties of the device by stretching and compression up to the value of the preload. The part with the low grade inclination models the absorbing of the mechanism by compression behind the preload.
Figure 18.45. Linear approximation of the characteristics out of the definition region

Remark. The user must keep in mind that a linear approximation of the characteristics takes place for abscissa value out of the definition region, Figure 18.45.

Figure 18.46. Joint torque

<table>
<thead>
<tr>
<th>X</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 _d_tension_angle</td>
<td>pretension_torque*(rear_drive_key+1)/2</td>
</tr>
<tr>
<td>2 _d_tension_angle+pretension_torque/c_torsion/100</td>
<td></td>
</tr>
<tr>
<td>3 _d_tension_angle+pretension_torque/c_torsion/100+1</td>
<td>([pretension_torque<em>c_torsional</em>(rear_drive_key+1)^2]</td>
</tr>
</tbody>
</table>

a)
### Table 18.47

<table>
<thead>
<tr>
<th>X</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>d_tension_angle - pretension_torque / c_forsional / 100 - 0.1</td>
<td>pretension_torque + c_forsional * 0.1 * (1 - rear_drive_key) / 2</td>
</tr>
<tr>
<td>d_tension_angle - pretension_torque / c_forsional / 100</td>
<td>pretension_torque * (1 - rear_drive_key) / 2</td>
</tr>
<tr>
<td>d_tension_angle</td>
<td></td>
</tr>
</tbody>
</table>

b)

Figure 18.47. Mathematical models of joint torque enabled by \( \text{rear\_drive\_key}=1 \) (a) and \( \text{rear\_drive\_key}=-1 \) (b)

The joint torque is of the **List of forces** type, which includes two elements of the **Points (symbolic)** type, Figure 18.46, Figure 18.47.
18.1.1.4.2.2. Idler on a crank. A more detailed model

As opposite to the previous section, here the tension device is described in more details. The force element is attached to the crank in point A, and to $Base0$ in point B, Figure 18.48.

1. Path to the component file: \{UM Data\}\Caterpillar\Subsystems\idler_crank.dat.
2. Identifiers. In addition to parameters in Table 18.10 and Table 18.11, some identifiers are user for parameterization of the model geometry, Table 18.13, Figure 18.48.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$l_{crank_spring}$</td>
<td>(m) Distance between the crank/hull joint and point A.</td>
</tr>
<tr>
<td>$dx_tspring$, $dz_tspring$</td>
<td>(m) Position of B point relative to the wheel center</td>
</tr>
</tbody>
</table>

3. Bodies. See the previous section.
4. Joints. See the previous section. The difference consists in the lack of the joint torque.

5. Tension force element.

A bipolar force element $Tension spring$ is used for modeling the tension device. It realizes the properties mentioned in the previous section. The force characteristic is similar to that in Figure 18.48 by $rear\_drive\_key=1$.

\[ pretension + \text{heavi}(l\_tension\_spring-x) \cdot c\_tension\_spring \cdot (l\_tension\_spring-x) + \]
heavi(l_tension_spring+x)*(-c_tenstion_spring*100*(-l_tension_spring+x))

where $x$ is the element length, $l_{tension\_spring}$ is the length of unloaded element, $pretension$ is the identifier for the preload force, $c_{tenstion\_spring}$ is the spring constant; the Heaviside function is

$$\text{heavi}(x) = \begin{cases} 1, & x > 0 \\ 0, & x \leq 0 \end{cases}$$

The length of unloaded element is expressed in terms of geometric and force parameters of the model as

$$l_{tension\_spring} = \sqrt{(dx_{tspring}+dl_{crank\_spring}*sa)^2+(dz_{tspring}-dl_{crank\_spring}*ca)^2}+dl_{tension\_rod}-pretension/c_{tension\_spring}/100$$

This expression consists of three parts.

- $\sqrt{(dx_{tspring}+dl_{crank\_spring}*sa)^2+(dz_{tspring}-dl_{crank\_spring}*ca)^2}$ is the length of element by zero value of object coordinates;
- $dl_{tension\_rod}$ is an additional change in the element length; the length of the element is increased with the parameter $dl_{tension\_rod}$, so that change of the latter can be used for generation of the desired tension of the track in case track links with rigid joints;
- $pretension/c_{tension\_spring}/100$ is an additional term which provides the zero value of force for zero value of elongation $dl_{tension\_rod}=0$. 
18.1.1.4.3. Sprocket

18.1.1.4.3.1. Geometrical parameters of sprocket

The following track joint types are implemented in UM:
- rigid joints, Figure 18.49a,
- one flexible joint (bushing) for a track link, Figure 18.49a,
- two parallel flexible joints for a track link, Figure 18.49b.

Figure 18.49. Fragments of track models: track links with one joint (a) and with parallel joints (b)
Main parameters specifying sprocket geometry are (Figure 18.50, Figure 18.51):

- number of teeth $Z$;
- wheel radius on pin centers $R_s$;
• wheel radius of tooth tops $R_o$;
• tooth height over the pin center radius $h = R_o - R_s$.
• wheel step $t_w$;
• track step $t_t$;
• distance between parallel joint of links $L_J$;
• step ratio $D = t_w / t_t$

The user should set three parameters from this list: $Z$, $t_t$ and $D$. Other parameters for a track with one joint for a link are computed according to formulas

$$t_w = D t_t,$$
$$R_s = \frac{t_w}{2 \sin \beta / 2} = \frac{t_w}{2 \sin \pi / Z}.$$

In the case of a track with parallel joints, the $R_s$ radius is computed according to the formula (Figure 18.51)

$$t_w - L_J + L_J \cos \frac{\beta}{2} = \sin \frac{\beta}{2} \sqrt{4R_s^2 - L_J^2},$$

i.e.

$$R_s = \frac{1}{2} \sqrt{\frac{(t_w - L_J + L_J \cos \beta / 2)^2}{\sin^2 \beta / 2}} + L_J^2.$$

In addition, sprocket geometry requires the description of tooth profile.

**18.1.1.4.3.2. Automatic generator of sprocket tooth profiles**

Figure 18.52. Template of sprocket profile for track with one joint a link
Figure 18.53. Templates of sprocket profile for track with parallel joints

Some sprocket tooth profiles can be generated in UN automatically, Figure 18.52, Figure 18.53.

To generate a profile, the following steps are necessary.

1. Run input program UM Input.
2. Open a tool for generation of profiles by the Tools | Generator of sprocket tooth… menu command.
3. Select a type of profile from the drop-down list:
Figure 18.54. Parameters of sprocket profiles

4. Set profile parameters.
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- **Sprocket, 1 joint, #1**, Figure 18.52, Figure 18.54a; list of parameters:
  - number of teeth $Z$;
  - Sprocket step $L_{\text{Link}} = t_w$, mm;
  - Toot height over the pin center radius $h = R_0 - R_s$, mm;
  - radius of tooth root $R$, mm;
  - tooth central angle $\gamma$, degrees;
  - tooth wedge angle $\psi$, degrees;
- **Sprocket, 2 joint, #1,2**, Figure 18.53, Figure 18.54b; list of parameters:
  - number of teeth $Z$;
  - Sprocket step $L_{\text{Link}} = t_w$, mm;
  - Toot height over the pin center radius $h = R_0 - R_s$, mm;
  - distance between parallel joint of links $L_J$, mm;
  - radius of pin $R_P$, mm;
  - tooth profile radius $R_T$, mm;
  - radius of tooth root $R$, mm;
  - tooth angle $\mu$ measured at the trimming point of circles $R_T$ and $R_P$, degrees.

Use the \( \equiv \) button to compute and plot the profile.

Save the profile to file by the \( \equiv \) button.

The buttons \( \equiv \-equiv\) are used for getting either the current profile plot (Figure 18.54) or a plot template, Figure 18.52, Figure 18.53.

**Remark.** Length parameters are set in millimeters, but they are converted to meters by saving in file.

### 18.1.1.4.3.3. Creation of profile by curve editor

![Curve editor](image)

Figure 18.55. Tooth profile in the curve editor

A tooth profile can be created in the built-in curve editor. The profile is specified by a sequence of points in the system of coordinates $x_t,y_t$. The origin of this system of coordinate is lo-
cated on the circle passing through the pin profile centers in the middle of center the tooth root, Figure 18.50, Figure 18.55. Description of the curve editor functions can be found in Chapter 3, Sect. Object constructor | Curve editor.

Figure 18.56. Creation and modification of sprocket and pin profiles

The buttons in the Sprocket and Track tabs of the track wizard are used to call the editor, Figure 18.56.

Coordinates are set in meters.

One of the possible ways of creating the profiles consists in use of external editors. Coordinates of points should be written in a text file in two columns with the space character as a separator. The first column contains abscissa values in the increasing order. Example:

```
-0.0607102  0.0158691
-0.0547835  0.0170649
-0.0315034  -0.0174493
 0.0315034   -0.0174493
 0.0547835   0.0170649
 0.0607102   0.0158691
```

Figure 18.57. Spline interpolation of a curve
The file can be read in the curve editor by button. A small step size for points along abscissa should be used but not less than one millimeter. It is recommended to use the spline interpolation of selected section or the curve, Figure 18.57.
18.1.1.4.3.4. Template of sprocket

Figure 18.58. Identifiers for geometric parameters of sprocket

1. Path to the component file: {UM Data}\Caterpillar\Subsystems\sprocket.dat.
2. Standard identifiers, Table 18.14, Figure 18.58.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>wguide</td>
<td>Width of a slot in the wheel for run of track teeth</td>
</tr>
<tr>
<td>hguide</td>
<td>Depth of a slot in the wheel for run of track teeth</td>
</tr>
<tr>
<td>xcsprocket</td>
<td>Longitudinal coordinate of the sprocket center</td>
</tr>
<tr>
<td>zcsprocket</td>
<td>Vertical coordinate of the sprocket center</td>
</tr>
<tr>
<td>wsprocket</td>
<td>Sprocket width</td>
</tr>
<tr>
<td>rsprocket</td>
<td>Wheel radius on pin centers Rs, Figure 18.51</td>
</tr>
<tr>
<td>traction_torque</td>
<td>Standard identifier for traction or brake torque applied to the sprocket</td>
</tr>
</tbody>
</table>
3. **Bodies.**

The model contains one body *Sprocket*, marked by the text attribute of C-type: *Sprocket*, Figure 18.59. The attribute is used by the program for identification of the body corresponding to the sprocket. Inertia parameters are presented in Table 18.15.

**Table 18.15**

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>m_sprocket</em></td>
<td>100</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td><em>ix_sprocket</em></td>
<td>15</td>
<td>(kg m²) Moment of inertia relative to the axis in the wheel plane</td>
</tr>
<tr>
<td><em>iy_sprocket</em></td>
<td>20</td>
<td>(kg m²) Moment of inertia relative to the rotation axis</td>
</tr>
</tbody>
</table>

4. **Joints.**

The model includes one rotational joint *jSprocket* connecting the Sprocket body with *Base0*. By adding the component to the track model, the body *Base0* is automatically replaced by the local hull of the track.

**Remark.** Sprocket component does not include a tooth profile. The user assigns a profile with the help of the track wizard.
Three components are delivered as standard ones. The components differ in the joint type:

- **TrackLink_Rigid** with a rigid joint, Figure 18.60a;
- **TrackLink_Bushing** with a flexible joint (bushing), Figure 18.60b;
- **TrackLink_Parallel** with two parallel flexible joints (bushings), Figure 18.60c.

**Standard elements**

1. **Standard identifiers.** Any component describing a track link must contain the standard identifiers, Table 18.16.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>ltracklink</td>
<td>Track link length</td>
</tr>
<tr>
<td>wtracklink</td>
<td>Track link width</td>
</tr>
<tr>
<td>htracklink</td>
<td>Track link height</td>
</tr>
<tr>
<td>wsprocket</td>
<td>Sprocket width (track link width on pins)</td>
</tr>
</tbody>
</table>

Figure 18.61. Standard text attribute of a track link
2. **Standard element**: a text attribute. The track link body must be marked by the text attribute of C-type: *TrackLink*, Figure 18.61.
18.1.1.4.4.1. Track link with rigid joint

The component models a track link with a rigid rotational joint. The joint model includes both friction and elastic torques, which can be used optionally.

1. **Path to the component file:** `{UM Data}\Caterpillar\Subsystems\TrackLink_Rigid.dat`.

2. **Bodies.**
   The model includes one body *TrackLink*, marked by the text attribute of C-type: *TrackLink*. Inertia parameters are set by identifiers, Table 18.17.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>m_track_link</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td>ix_track_link, iy_track_link, iz_track_link</td>
<td>(kg m²) Moments of inertia relative to central axis</td>
</tr>
</tbody>
</table>

3. **Joints**
   The model contains two joints:
   - an internal joint of body *TrackLink* with six d.o.f., which is removed automatically by adding the link to the track model;
   - rotational joint *jTrack link* connecting the track link with an external body; by adding the link to the track model the next link in the track is automatically assigned as the second body of the joint.

4. **Pin position** (external, internal)

   Figure 18.62. Internal (a) and external (b) pin positions

The type of the pin position is specified by the identifier *pin_key*: +1 for the internal and -1 for the external positions, Figure 18.62.
5. Joint force

The joint torque allows modeling both a friction and a linear viscous-elastic torque in the joint in parallel, Figure 18.63.

**Friction torque.** The friction torque value is set by the identifier \( \text{LinkFriction} \) (Nm). In the sticking mode, torsion stiffness and damping are set by the identifiers \( c\text{StiffLink} \) (Nm/rad), \( c\text{DissLink} \) (Nms/rad). To remove the friction, numeric values of all three parameters should be set to zero.

**Viscous-elastic torque** is specified by the stiffness and damping constants \( c\text{LinkBushing} \) (Nm/rad), \( d\text{LinkBushing} \) (Nms/rad). A possible preload torque is set by the identifier \( \text{LinkPreload} \) (Nm) – this is the torque for zero value of the joint coordinate. To remove the linear torque, numeric values of all three parameters should be set to zero.
18.1.1.4.4.2. Track link with flexible joint (bushing)

The component models a track link with a flexible joint or bushing.

Path to the component file:
{UM Data}\Caterpillar\Subsystems\TrackLink_Bushing.dat.

The component description is similar to the track link with rigid joint. The main difference is that the rotational joint is replaced by a linear bushing, Figure 18.64.

Stiffness constants for directions of shift and rotation are set by identifiers

- $c_x$ (N/m, longitudinal stiffness),
- $c_y$ (N/m, lateral stiffness),
- $c_z$ (N/m, stiffness by vertical shift)
- $c_{ax}$ (Nm/rad, torsion stiffness about the longitudinal axis),
- $c_{ay}$ (Nm/rad, torsion stiffness about the lateral or joint axis),
- $c_{az}$ (Nm/rad, torsion stiffness about the vertical axis).

Damping constants are specified with the help of damping ratios $\beta_x$ for shifts and $\beta_a$ for rotations. Default values of these parameters are 0.1. Detailed information about the notion of the damping ratio can be found in Chapter 2, Sect. Methodology of choice of contact parameters.

For obtaining a desired value of the track tension, a longitudinal force is used parameterized by the standard identifier $track\_tension$. 
A preload torque, i.e. the torque value for zero rotation about the lateral axis, is set by the identifier \textit{torque\_y\_preload}.
18.1.1.4.4.3. Track link with two parallel bushings (double pin)

The component is modeled a track link with parallel bushings (double pin). It is assumes that pins of two neighbor links are rigidly connected by a clamp. This construction is considered as an additional rigid body.

Thus, the model description differs from the track link with one bushing by the following elements:

- additional body $Link-Link$,
- joint with six d.o.f. $jBase0\_Link-Link$
- additional bushing connecting the body $Link-Link$ with an external body (the next link).

![Figure 18.65. Geometrical parameters](image)

The model contains two additional standard identifiers, Figure 18.65:

- $pin\_distance$ (m) is the distance between pins of neighbor links, $L_j$ in Figure 18.51;
- $r\_pin$ (m) is the pin radius.

Path to the component file:

{UM Data}\Caterpillar\Subsystems\TrackLink\Parallel.dat.
18.1.1.4.5. Roller

Figure 18.66. Model of a roller

A track can include any number of rollers. In particular, none roller can be presented.

1. Path to the component file: {UM Data}\Caterpillar\Subsystems\roller.dat.
2. Standard identifiers, Table 18.18.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>wguide</td>
<td>Width of a slot in the roller for run of track teeth</td>
</tr>
<tr>
<td>hguide</td>
<td>Depth of a slot in the roller for run of track teeth</td>
</tr>
<tr>
<td>rroller</td>
<td>Roller radius</td>
</tr>
<tr>
<td>wroller</td>
<td>Roller width</td>
</tr>
</tbody>
</table>

Figure 18.67. Roller body parameters
3. **Bodies.**

The model contains one body *Roller*, marked by the text attribute of the C-type: *Roller*, Figure 18.67. This attribute is used for identification of the roller by the program. Inertia parameters are presented in Table 18.19.

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>m_roller</em></td>
<td>20</td>
<td>(kg) Mass</td>
</tr>
<tr>
<td><em>ix_ roller</em></td>
<td>2</td>
<td>(kg m²) Moment of inertia relative to the axis in the roller plane</td>
</tr>
<tr>
<td><em>iy_ roller</em></td>
<td>1</td>
<td>(kg m²) Moment of inertia relative to the rotation axis</td>
</tr>
</tbody>
</table>

4. **Joints.**

The model included one rotational joint *jRoller* connecting the roller with *Base0*. By adding the component to the track model, the body *Base0* is automatically replaced by the local hull of the track.
18.1.2. Development of user’s components

In this section, we consider an example of development of a new component. Note that often new components as obtained as a result of modification of existing ones. For instance, the user can change images of elements in the components.

18.1.2.1. Development of a torsion bogie with three wheels

Figure 18.68. An analogue of the developing bogie

1. Selection of an analogue and creation of a file with new component.
   Consider a torsion bogie with two wheels as an analogue of a new component, Figure 18.68, Sect. 18.1.1.4.1.5. "Torsion two-wheel bogie", p. 18-27. Our goal is to add the third road wheel connected with the frame by a rotational joint.
   - Run UM Input
   - Create a new UM objects by the button on the tool panel or by the File | New object menu command.
   - Read the file \{UM Data\}\Caterpillar\Subsystems\bogie_2wheel_1arm.dat. by the button on the tool panel or by the Edit | Read from file… menu command.
     The program adds to the object a subsystem with the bogie shown in Figure 18.68 as well as the list of selected identifiers.
   - Save the object to file as a new component in any directory, for example \{UM Data\}\Caterpillar\Subsystems\bogie_3wheel_1arm.dat by the button or by the File | Save as component command.
     Note that the name of the file will be accepted as the name of the component. File extension must be *.dat.
2. Modification of the bogie model

- Select the subsystem Subs1 in the list of elements and start its editing by the **Edit** button in the inspector, Figure 18.69. A new window with the bogie description is opened.

![Figure 18.69. Component editing](image)

- Double click in the identifier wheel_base and change its value to 0.8, Figure 18.70.

![Figure 18.70. Change of bogie base](image)

- Double click in the identifier wheel_base and change its value to 0.8, Figure 18.70.

![Figure 18.71. Selection of a body](image)
**Chapter 18. Tracked vehicles**

- Select the *Road wheel rear* body, Figure 18.71, copy it by the button and rename to *Road wheel central* (do not forget to press Enter after changing the name). Change the body position in the list by the mouse, Figure 18.72.

  ![Figure 18.72. Change of body position in the list](image)

- Select the *jRoad wheel rear* joint, Figure 18.74, and copy it by the button. Rename the joint as *jRoad wheel central* and press Enter. Assign the second body *Road wheel central*. Set zero value of the longitudinal joint coordinate for body *Bogie frame*, Figure 18.73 right, Figure 18.74.

  ![Figure 18.73. Selection of a joint and parameters of new joint](image)

![Figure 18.74. New kinematic pair](image)
• The model is ready, Figure 18.75. Accept modifications in the subsystem by the corresponding button in the **Close subsystem** window, Figure 18.76.

• Save the modified model by the button or by the **File | Save as component...** menu command.

• Close the model window without saving.

After development of the model, it must be registered (Sect. 18.1.3. "Registration of new TV components", p. 18-66).
18.1.3. Registration of new TV components

New components of TV elements should be registered before they can be used by development of a track model.

The following components can be registered in the current UM version, Sect. 18.1.1.4.2. "Idler and tension device", p. 18-31:
- suspension unit
- idler with tension device
- track link

The following steps are necessary for the registration.

1. Open UM Input. If it is already open, close all UM objects.

![Figure 18.77. Tool for registration of TV components](image)

2. Open the “Components of track vehicle” window by the Tools | Components of track vehicle… command, Figure 18.77. If the command is not enabled, verify whether all objects are closed.

3. Select a necessary tab in the window, e.g. Suspension, and open a file with the component by the button.

4. To exclude the component from the list, use the button.

5. Use the Accept or Cancel buttons to update the registry or to skip modifications.

![Figure 18.78. List of standard and registered suspension units](image)
After registration, the components become available in the corresponding list of components of the wizard of track model, Figure 18.78.

**Remark.** Components are registered on the local machine. To use it on another computer, the component must be registered there in the same manner.
18.1.4. Development of TV model

A special tool named ‘Wizard of track’ is used for automatic generation of a track model. Consider detailed a sequence of steps, which are necessary for generation of a TV.

We will use some parameters of a Russian high-speed crawler transporter.

18.1.4.1. Preparing step

If the model cannot be developed with use of standard components, the user should create own components and register them. Three types of TV parts are available for these purposes:

- suspension units
- idler with tension device
- track link

The user can change images in the standard components, add new force elements and modify existing ones.

It is necessary to create files with a sprocket tooth and, if necessary, a pin profile, Sect. 18.1.1.4.3.2. "Automatic generator of sprocket tooth profiles", p. 18-45, Sect. 18.1.1.4.3.3. "Creation of profile by curve editor", p. 18-48.

18.1.4.2. Adding a track subsystem

1. Create a new UM object in UM Input.
2. Add a Caterpillar subsystem:
   - select the Subsystems item in the list of elements
   - click the right mouse button an select the Add element to group “Subsystems” | Caterpillar command, Figure 18.79.

As a result, a Wizard of track appears in the object inspector. The following tabs are available on the Parameters sheet.
• Structure
• Suspension
• Sprocket
• Idler
• Rollers
• Track

18.1.4.3. Track structure

![Track structure parameters](image_url)

Figure 18.80. Parameters of track structure

The following parameters should be set on the **Structure** tab, Figure 18.80:

- position of the track **Left/Right**
- number of suspension units
- number of rollers (can be zero)
- number of track links
18.1.4.4. Suspension

**Suspension** tab.

1. Select the type of suspension from the drop-down list.
2. Set geometrical parameters of the suspension in meters, Sect. 18.1.4.1.1. "Standard elements and identifiers of suspension subsystems", p. 18-10, Table 18.1

   - **R** is the radius or road wheels corresponding to the standard identifier *roadwheel*
   - **W** is the width of road wheels corresponding to the standard identifier *wroadwheel*
   - **Xc1…** are the longitudinal coordinates specifying positions of suspension units; number of coordinates is equal to the number of the units in the **Structure** tab; the coordinate values are automatically assigned to the standard identifiers *xbogie* in each of the subsystems.

![Figure 18.81. Suspension parameters](image)

**Figure 18.81. Suspension parameters**

- Click on the **Generate** button to create the suspension model; the suspension image appears in the animation window, Figure 18.82.
- Use the **Identifiers | Suspension** tab for modification of numerical values of selected identifiers.
- It necessary, parameters of the subsystem can be changed. After changing, click the **Generate** button.

![Figure 18.82. Generated suspension](image)

**Figure 18.82. Generated suspension**
18.1.4.5. Sprocket

Tab Sprocket

1. Assign a tooth profiles with the built-in curve editor:
   - open the editor by the button
   - read a preliminary created file with profile by the button.

2. Set the number of teeth, sprocket/track step ratio $t_w/t_t$ as well as geometric parameters, see Table 18.14:
   - Width parameter corresponds to the $w_{sprocket}$ identifier
   - $X_c, Z_c$ are the longitudinal and vertical coordinates corresponding to the identifiers $x_{sprocket}, z_{sprocket}$

3. The button is used for the preliminary view of the sprocket.

4. The Generate button adds the sprocket to the model, Figure 18.84.

**Remark.** Sprocket radius is computed automatically at the last step of development of a track model, when all geometric parameters of the model are defined.
18.1.4.6. Idler

Idler tab, Figure 18.85

1. Select a type of the tension mechanism from the drop-down box.
2. Set geometrical parameters of the idler in meters, Table 18.10.
   - \( R \) is the idler radius corresponding to the standard identifier \( r_{idler} \)
   - \( W \) is the idler width, the standard identifier \( w_{idler} \)
   - \( X_c, Z_c \) are the longitudinal and vertical coordinates of the idler center, the standard identifiers \( x_{idler}, z_{idler} \).
3. The Generate button adds the idler to the model, Figure 18.86.
4. Set numerical values of the tension device parameters.

Figure 18.85. Idler parameters

Figure 18.86. Adding idler to model
18.1.4.7. Rollers

**Rollers** tab, Figure 18.87

1. Set geometrical parameters for rollers in meters, Table 18.10.
   - R is the roller radius, the standard identifier *rroller*
   - W is the roller width, the standard identifier *wroller*
   - Xc…, Zc… are the longitudinal and vertical coordinates of roller centers.

2. The **Generate** button adds rollers to the model.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>R</td>
<td>0.12</td>
</tr>
<tr>
<td>W</td>
<td>0.3</td>
</tr>
<tr>
<td>Xc1</td>
<td>1.9</td>
</tr>
<tr>
<td>Zc1</td>
<td>1.05</td>
</tr>
<tr>
<td>Xc2</td>
<td>4.9</td>
</tr>
<tr>
<td>Zc2</td>
<td>1.05</td>
</tr>
</tbody>
</table>

Figure 18.87. Parameters of rollers
18.1.4.8. Track

Model of the track consisting of given number of links is created on the Track tab, Figure 18.88. The track can be generated only if all other elements are correctly described by the user and added to the model: suspension units, sprocket, idler, rollers. According to the geometrical parameters including coordinates of wheel centers and radii, UM compute an enveloping curve for the track chain. The estimated length of this curve is set in the Length of envelope box. By the button, the user may get a window with the envelope image, Figure 18.89.

Figure 18.88. Track tab in case of non-complete and complete state

Figure 18.89. Track curve
If specification of track elements is not complete (e.g. if the idler is not added to the model), and UM cannot generate the enveloping curve, the message ‘Description is not complete or incorrect’ is visible. The **Summary** button displays comments to the errors.

If all geometrical parameters are specified but the difference between the estimated \( L_{\text{est}} \) and the real \( L = n_{\text{link}} L_{\text{link}} \) lengths (\( n_{\text{link}} \), \( L_{\text{link}} \) are the number and length of links) exceed the length of a track link (‘Current error in length’), the track cannot be generated as well. The user should correct some geometrical parameters, e.g. coordinates of the idler center, or change the number of links to avoid the lack or redundancy of links in the chain.

The program computes a recommended length of the track link (‘Estimation of track length’), which matches the track curve. If the recommended length of link differs from the specified one on a fraction of millimeter like in Figure 18.88, right, it is desirable to correct the length \( L \) to improve the closure condition of the track.

If all geometrical parameters including the track length are correct, the **Generate** button becomes available, and the user may add the links to the track model.

The following steps are necessary.

1. Choose the track link type from the list.
2. Set the joint type if the link type differs from the three standard ones.
3. Specify the pin profile with the curve editor by the **(add)** button.
4. Set the length, width and height of the link (\( L \), \( W \), \( H \) parameters, m).
5. Add links by the **Generate** button, Figure 18.90.

**Figure 18.90. Track model**

### 18.1.4.9. Completion of track model. Adding dampers

If necessary, dampers (shock absorbers), stops and other force elements can be added to the track model, Figure 18.91. Standard tools for description of force elements are used for this purpose.
Dampers can be modeled by bipolar force elements. An example of damper characteristics is shown in Figure 18.92. To create such a model, the user should set

- bodies connected by the damper;
- coordinates of attachment points in SC of each of two bodies;
- type of force element: **Points (numeric)**;
- velocity (v) as abscissa type;
- type of characteristic: compression positive (i.e. the positive velocity on the plot corresponds to the compression of the element);
  - force vs. velocity points in the order corresponding to the growth of the velocity; units are N for force and m/s for velocity.
Figure 18.92. Damper as a bipolar force element

It is recommended to use the **Frictional** type of bipolar force for modeling frictional dampers.

See Chapter 2 of the user’s manual for additional information about modeling of force elements in UM.
18.1.5. Finalization of TV model

In the previous section we described the development of a track model. Here we consider a method for finalization of a complete TV model, which requires adding a hull, a second track, connecting tracks with the hull and, if necessary, adding transmission elements.

18.1.5.1. Adding a hull

To add a hull to the model of TV, make the following steps.

1. Create a graphic object for the hull image. The image can be both simplified and more realistic or imported from CAD software, Figure 18.93. The image is not important for simulation results but it influences the quality of visualization of the TV model.

2. Add a body corresponding to the hull to the TV model, assign the image. Set inertia parameters (mass, moments of inertia relative to the SC with the origin in the hull center of mass,
coordinates of the center of mass). It is recommended to choose the hull-fixed system of coordinates in such a way that it coincides with SC0 for zero values of coordinates, Figure 18.94. The image should be shift according to this choice.

**Remark 1.** Please note that moments of inertia of bodies are specified in the central SC (i.e. the origin is located in the center of gravity of the body) which axes are parallel to the axes of the body-fixed SC.

**Remark 2.** For internal identification of the hull by the program it is recommended to use the standard name Hull or a text attribute with the same name, see Sect. 18.1.6.2.8. "Steps after adding transmission model", p. 18-92.

![Inertia parameters of a hull](image)

**Figure 18.95. Inertia parameters of a hull**

If inertia parameters of the hull are not known exactly or/and can be modified, they must be parameterized, Figure 18.95.
Figure 18.96. Joint introducing six degrees of freedom of a hull relative to Base0

3. Add a joint with six d.o.f. specifying coordinates of the hull relative to SC0 (Base0), Figure 18.96. The first body in this joint must be Base0, the second one is the hull.

![Diagram showing joint connection](image)

Figure 18.97. Model of TV with the hull

As a result, the hull is added to the model of the TV but it is still not connected with the track. Moreover, the TV contains so far only one (left) track located in the middle of the hull, Figure 18.97.

18.1.5.2. Connection of track with hull

To connect joint and force elements described in the track model with the hull of the TV, it is necessary to fix the local hull of the track with the hull of the TV, Sect. 18.1.1.4.1.1. "Standard elements and identifiers of suspension subsystems", p. 18-10. As we have mentioned, the joints and force elements are firstly connected with the local hull of the track, and the latest step will connect them directly with the hull of TV.
Fixing the local hull relative to the hull of TV is made by a joint with zero number of d.o.f., Figure 18.98:

- add a joint;
- assign the hull as the first body and the local hull as the second one;
- set joint type: **Generalized**;
- add one elementary transformation and set its type tc (translation constant);
- set lateral shift of the track relative to the hull (a half of the gauge) in the ey box, Figure 18.98.

The result is shown in Figure 18.99.

It is recommended using the *gauge* identifier for the parameterization of the TV gauge value, see Sect. 18.1.6.2.8. "Steps after adding transmission model", p. 18-92.

**18.1.5.3. Adding the second track**

To complete the TV model, it is necessary to add the second track:

- open the first track in the inspector;
- copy the subsystem by the **button;**
set track position **Right**, Figure 18.100;
- copy the joint fixing the local hull of the left track with the hull of TV;

set the local hull of the right track as the second body;
- change sign of the lateral shift in the **ey** box, Figure 18.101.
18.1.5.4. Correction of vertical TV position

Figure 18.102. Shift the model upwards

To avoid intensive transient processes by simulation, it is recommended to shift the TV model upwards on the link height, Figure 18.102.

![Figure 18.103. Vertical shift of TV model](image)

To shift the model upwards, open the joint specifying coordinates of the TV hull relative to the SC0 and set the vertical coordinate in the Geometry | Body1 tab, Figure 18.103.

![Figure 18.104. Model of TV](image)

The model of TV is ready, Figure 18.104. Using this model, the user can analyze loading the suspension and ride comfort, as well as optimize suspension parameters, etc.
18.1.6. Transmission and steering system

The model of transmission includes an internal combustion engine (ICE), powertrain and steering mechanism. Elements of transmission are detailed described in Chapter 22 "UM Driveline". Here we consider database of TV transmissions, which differ on the steering system.

18.1.6.1. Adding transmission from database

Database of TV transmissions is located in the directory {UM Data}\Caterpillar\Driveline and includes files listed in Table 18.20.

<table>
<thead>
<tr>
<th>Menu item</th>
<th>File name</th>
<th>Model description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clutch-brake steering</td>
<td>Clutch – Brake.dat</td>
<td>18.1.6.3</td>
</tr>
<tr>
<td>Planetary steering</td>
<td>Planetary steering.dat</td>
<td>18.1.6.4</td>
</tr>
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<td>Controlled differential steering</td>
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<tr>
<td>Double differential steering HSD *)</td>
<td>Double differential steering HSD.dat</td>
<td>18.1.6.10</td>
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</table>

*) Hydrostatic drive

![Figure 18.105. Transmission with Clutch-Bake steering mechanism](image)

The Tools | Add transmission mechanism menu item is used to add a transmission to the TV model, Figure 18.106. After selection of the desired transmission, the model will be added to the TV model and several steps of TV-transmission coupling will be done automatically. List of transmission models and the corresponding data files are collected in Table 18.20.
18.1.6.2. Common element of standard transmission models

We describe here elements of transmissions presented in every of the standard UM models. Consider the file Clutch-Break.dat as an example.

The file contains an object which includes one subsystem representing the transmission model. The ‘driveline’ text attribute identifies the transmission, Figure 18.107.
Apart from the subsystem, the object contains a joint (Figure 18.108). The first joint body is not assigned, and the second one is the fictitious driveline body Hull fix, 18.1.6.2.1 "Fictitious body", p. 18-86. The joint connects rigidly the fictitious body with the TV hull after adding the transmission to the TV model.

Now consider elements of the subsystem.

18.1.6.2.1. Fictitious body

The fictitious body in the transmission model replaces the TV hull. This means that all joints and force elements connected to the hull are connected to the fictitious body instead. When the transmission is added to the TV, the fictitious body is fixed to the TV hull by a special joint, Figure 18.108.

The fictitious body has zero inertia parameters as well as an internal joint with six degrees of freedom (Figure 18.109), which is ignored after fixing of the body with the TV hull. Please note that a body with an internal joint is created by the button 🏷️.
18.1.6.2.2. Internal combustion engine

ICE parameters are defined in simulation program and detailed described in Chapter 22 of the user's manual. In the simplified transmission models the engine is described by one body and one joint.

The body accepts the inertia properties of the engine shaft, connecting rod and other joint parts. It is important to specify accurately the moment of inertia relative to the rotation axis, which is parameterized by the identifier i_icerotor.

The body must be marked by the text attribute ice, Figure 18.110, according to which the program recognize the ICE in the model.

Please note that the sequence of rotations yaw, pitch, roll (3,2,1) is assigned to the body through the Coordinates (PP) drop down menu. PP is the abbreviation for the Park Parallel solver. The engine shaft rotates often rapidly, and this type of coordinates improves the simulation step size.

The revolute joint specifies the rotational degree of freedom for the engine shaft and simultaneously sets the engine torque by the standard identifier ice_torque, Figure 18.111.
Figure 18.111. Joint specifying rotation of the engine shaft and engine torque

18.1.6.2.3. Main clutch, torque converter

Either the main clutch or the torque converter is used for the engine-gearbox coupling, Figure 18.112.

The main clutch is modeled by a scalar torque of the frictional type. The force element must be marked by the text attribute `clutch_coupling` for automatic identification of the element. The frictional torque is parameterized by an identifier with the default value `clutch_torque`. The identifier is used for setting the computed value of the torque in dependence of the pedal position.

The torque converter is also presented in the transmission model as a special force element. The element is marked by the text attribute `fluid_coupling`, Figure 18.112.
The user selects one of the two force elements as an active one before start of the simulation process, Figure 18.113.

18.1.6.2.4. Gearbox

A simplified model of a gearbox is presented by the special force element of the 'Mechanical converter of rotation' type, Figure 18.114.

Successful identification of the element by the program requires the standard text attribute of this element gearbox.

The force parameters in Figure 18.114 are set by identifiers, which default values are:

- `gearbox_ratio` is the value of gear ratio,
- `gearbox_stiffness` (Nm/rad) is the stiffness constant if the gearbox, which can be different for various gear ratios,
- `gearbox_efficiency` is the gearbox efficiency for every ratio.

The `rotation_sign` identifier with the value 1 or -1 is used for specifying a correct rotation direction, Figure 18.114.
18.1.6.2.5. Stopping brake

The stopping brake is modeled by two joint torques of the 'Frictional' type, Figure 18.115. The torques brake input shafts of the final drives. The recommended (default) identifier for parameterization of the torque is brake_torque. In the case of the clutch-brake steering system, the stopping brakes are used for the vehicle steering. Application of the right brake leads to the right turn of the vehicle. The standard identifiers turn_right (equals 1 for the right turn) and turn_left (equals 1 for the left turn) activate the necessary brake according to the expressions (Figure 18.115)

\[ \text{brake_torque} \times (1 - \text{turn_right}), \]
\[ \text{brake_torque} \times (1 - \text{turn_left}). \]

Figure 18.115. Brake torques

18.1.6.2.6. Final drive

The final drives are modeled by the special force elements of the 'Mechanical converter of rotation' type, Figure 18.116. Consider some features of the element descriptions:
- the second body is the External one; the drive wheels (sprockets) are assigned automatically by adding the transmission to the TV model;
- the elements are marked by the text attributes Left sprocket (left final drive) and Right sprocket (left final drive), which allows the program identifying the left and right elements;
- element parameters set by identifiers.
18.1.6.2.7. Identifiers

The model of transmission contains identifiers, which are used for the TV control. Three types of identifiers are used:

**Control identifiers** (Figure 18.117) used by the simulation program for the direct transmission control.

**Identifiers parameterizing model elements** are also used for control the transmission both by the program and by the user. Some of these identifiers are mentioned above. Consider here the list of main identifiers.

*Gauge* is used for specifying sizes and positions of elements such that one transmission model can be used for models of TV with different gauge value.

*Gearbox_ratio* is the gearbox ratio value. The identifier is changed by the program according to the current value of the control identifier *gearbox_position*.

*Brake_torque* is the identifier of the stopping brake torque. The numeric value of this identifier is assigned by the program according to the position of the brake pedal specifying be the control identifier *brake_position*.

*Ice_torque* is the engine torque. The torque is computed according to the ICE model in dependence on the throttle position specified by the control identifier *throttle_position*. 
Clutch_torque is the value of the main clutch torque. The torque is computed according to the current value of the control identifier clutch_position.

Sprocket_front is equal to 1 for the front-drive TV and -1 for the rear-drive TV. The identifier is used for parameterization of the transmission geometry.

Turn_right (turn_left): value 1 corresponds to the left (right) turn of TV otherwise the value is 0.

Identifiers computing transmission ratios give the program general information about conversion of the engine speed to the TV speeds. For instance they are used for internal evaluation of the turn radii.

Main_ratio (km/h / rpm) is the ratio of TV speed to the engine speed for the gearbox ratio equals to 1. In the case of the clutch-brake steering system it is computed as
\[ r_{\text{sprocket}}/\text{final}_ratio \times 3.6 \times \pi/30. \]
where r_sprocket is the drive wheel radius.

Transmission_ratio (km/h / rpm) is the ratio of TV speed to the engine speed for the given value of the gearbox ratio, i.e.
\[ \text{transmission}_ratio = \text{main}_ratio/\text{gearbox}_ratio. \]

Steer_ratio (km/h / rpm) is the ratio of the track speed decrease due to steering to the engine speed.

Steer_speed_ratio is the ratio of speeds of inner to outer tracks in turning. If we consider a "Maybach" steering system, it is computed as
\[ \text{steer}_\text{speed}_\text{ratio} = (\text{transmission}_\text{ratio}-\text{steer}_\text{ratio})/\text{transmission}_\text{ratio}. \]

18.1.6.2.8. Steps after adding transmission model

A type of the steering system according to Table 18.20 is assigned to the model. The type variable is used by the TV control algorithms by simulation.

The TV gauge value is set to the transmission subsystem. This step requires the identifier gauge both in the TV and the transmission models (Sect. 18.1.5.2. "Connection of track with hull", p. 18-80, Sect. 18.1.6.2.7. "Identifiers", p. 18-91).
3. The fictitious body of the transmission is connected rigidly with the TV hull (Sect. 18.1.6.2.1. "Fictitious body", p. 18-86). The hull is assigned to the first body in the corresponding joint (it is necessary to mark the hull body by the standard name or the text attribute Hull, Sect. 18.1.5.1. "Adding a hull", p. 18-78). In addition the joint specifies a shift according to the sprocket position relative to the hull, Figure 18.118.

4. The identifier sprocket_front value +1 or -1 is assigned according to the position of the drive wheel, Sect. 18.1.6.2.7. "Identifiers", p. 18-91.

1. External elements in the transmission subsystem are finalized by assignment of the second bodies, Figure 18.119. External elements are two final drives, and the second bodies are drive wheels. This step succeeds if the necessary text attributes are assigned to elements. Otherwise the step must be done manually.
If all steps succeed, the TV model with transmission is completed, Figure 18.120.

18.1.6.3. Clutch-Brake steering system

Description of the clutch-brake steering system can be found in [1], [2], [3]. For the vehicle turning, the steering clutch for the inside track is disengaged, and the brake is usually applied.

The most part of the transmission is described in Sect. 18.1.6.2. "Common element of standard transmission models", p. 18-85. Here we consider the models of steering clutches only.
The clutches are modeled by scalar torques of frictional type, Figure 18.121. The force elements connect the output shaft of the gearbox (body Shaft) with input shafts of the final drives (bodies Final shaft left and Final shaft right). The value of frictional torque is parameterized by the identifier *clutch_side_torque*. Engagement and disengagement of the clutches are made by the standard identifiers *turn_right* and *turn_left*, Sect. 18.1.6.2.7. "Identifiers", p. 18-91. Zero values of these identifiers lead to the straight-ahead motion. If *turn_right*=1, the right clutch is disengaged for the right turn, and *turn_left*=1 for the left turn.
18.1.6.4. Planetary gear steering system

See [1] for the mechanism description. Two planetary gear mechanisms are implemented in the model. The sun wheels are rigidly connected with the output shaft of the gearbox; all three parts are presented in the model by one body Output shaft, Figure 18.123. The input shaft of the final drive is rigidly connected with the carrier (bodies Carrier left and Carrier right).

Two clutches in engaged state connect the carriers and annuli of planetary mechanisms so that the planetary mechanism rotates as a rigid body. The clutches are presented in the model by
scalar torques *Steering clutch left* and *Steering clutch right*, Figure 18.121. Gear rings are bodies *Annulus left* и *Annulus right*. Brakes stop ring gears.

Description of brakes and clutches is similar to those in Sect. 18.1.6.2.5. "Stopping brake", p. 18-90 (brakes) and 18.1.6.3. "Clutch-Brake steering system", p. 18-94 (clutches).

In a straight line motion, the clutches are engaged and the brakes are released. For a turn, the clutch on the inner track is disengaged and the brake is applied, which lead to decrease of the carrier speed.

Consider a model of the planetary gears. For simplified modeling, a special force element of the *Planetary gearing* type is used, Figure 18.124.

Radii of gears are parameterized, which allows specifying the model geometry. Main ratios are computed in the list of identifiers:

- *annulus_ratio* is the gear ratio for the braked sun wheel;
- *sun_ratio* is the gear ratio for the braked annulus wheel.

It is important that the *sun_ratio* identifier is equal to the speed ratio of the inner track to the outer one in steering [1].
18.1.6.5. Controlled differential steering system

See description of the mechanism in [1], [2], [3].

The most part of the mechanism is described in Sect. 18.1.6.2. "Common element of standard transmission models", p. 18-85. Here we consider the model of the controlled differential, which consists of seven bodies:

- Differential housing;
- Gearbox;
- Controlled differential;
- Input shaft of final drive;
- Follower gear of differential;
- Driving gear;
- Double satellite;
- Output shaft of gearbox;
- Brake.
Sun wheel left and Sun wheel right are the controlled gears with rigidly connected input shafts of the finales drives;

Planet wheel 1 and Planet wheel 2 are two double satellites;

Controlled wheel 1 and Controlled wheel 2 are two controlled gears.

All these bodies have rotational degrees of freedom relative to the hull except of the satellites, which rotation axis are connected with the differential housing.

Figure 18.127. Transmission – crown wheel gearing

The special force element of the ‘Mechanical converter of rotation’ type is used for transfer of rotation from the output shaft of the gearbox to the crown wheel. The gearing ratio is parameterized by the differential_ratio identifier.

Figure 18.128. Differential gearings

Eight bevel gearings with ratio 1 are modeled the differential mechanism:

Gearing 1: gears Sun wheel left and Planet wheel 1;
Gearing 2: gears Sun wheel left and Planet wheel 2;
Gearing 3: gears Sun wheel right and Planet wheel 1;
Gearing 4: gears Sun wheel right and Planet wheel 2;
Controlled gearing 1: gears Planet wheel 1 and Controlled wheel 2;
Controlled gearing 2: gears Planet wheel 2 and Controlled wheel 2;
Controlled gearing 3: gears Planet wheel 1 and Controlled wheel 1;
Controlled gearing 4: gears Planet wheel 2 and Controlled wheel 2.

For steering, the brakes decelerate the rotation of the corresponding controlled gears up to the full stop. In the straight line motion, the brakes are released and the controlled differential works as a usual differential. In turn, the brake for the inner track is applied and decelerates the controlled gear. As a result, the rotation of the driving gear on the brake side is decelerated, and the opposite driven gear is accelerated; the TV keeps speed by turning. Simultaneous applying the brakes works as a stopping brake. The brakes are described by joint torques in joints for the controlled gears, Figure 18.129.

![Figure 18.129. Brake torque](image)

18.1.6.6. "Maybach" double differential steering system

This steering system was initially implemented during WWII in the German tank PzKw V Panther [2], [3].

The central elements of the steering system are two planetary gears, which summarize two flows of energy. The annuli of gears are rigidly connected with the output gearbox shaft, the Main shaft body. The carriers are connected with the input shafts of the final drives, bodies Carrier left and Carrier right. In a straight line motion, the sun wheels (bodies Sun wheel left, Sun wheel right) are fixed by the steering brakes, and the steering clutches (the special forces Steering clutch left, Steering clutch right) are disengaged.
In turning, the steering clutch for the inner track is engaged, the corresponding steering brake is released, and the sun wheel is rotated by the following chain: body Secondary shaft – simple gear (Steer gear left/right) – body Steering shaft left/right – sun wheel shaft. Rotation of the sun wheel makes the speed of the carrier and the inner track slower. Thus, steering reduces the TV speed.

Consider force elements except those described in Sect. 18.1.6.2. "Common element of standard transmission models", p. 18-85.

Secondary shaft coupling is the mechanical converter of rotation with the ratio equal to 1. The coupling drives the secondary shaft directly from the gearbox input shaft.

Planetary gearing left/right are the summarizing planetary gearings; the element description is similar to the planetary gears in Sect. 18.1.6.4. "Planetary gear steering system", p. 18-96.

Steer gear left/right are the simple gears driving the sun wheels in turnings. The gear ratio is parameterized by the identifier steering_ratio.

Steering clutch left/right are the scalar torques modeling the steering clutches. The clutch torques are described by the expressions

\[
\text{steering_clutch_torque*turn_left}, \\
\text{steering_clutch_torque*turn_right},
\]

where the identifier steering_clutch_torque parameterizes the torque of the engaged clutch.

Sun wheel brakes are described as joint torques in revolute joints jSun left/right by the expressions

\[
\text{jSun left/right}
\]
steering_brake_torque*(1-turn_left),
steering_brake_torque*(1-turn_right),

where the identifier brake_sunwheel_torque corresponds to the value of the applied brake.

Expressions for the torques produced by the clutches and brakes shows that in a straight line motion \((\text{turn}_\text{left} = \text{turn}_\text{right} = 0)\) the clutches are disengaged and the brakes are applied. For the left/right turn \((\text{turn}_\text{left} = 1/0, \text{turn}_\text{right} = 0/1)\), the left/right clutch is engaged and the left/right brake is released.

Note, that the main is the output shaft of the gearbox.

Consider two useful expressions. The first one is the relation between engine and track speeds for the locked sun wheel

\[
v = \frac{i_a}{i_{fin}i_{gb}} \omega = k_{main}\omega.
\]

Here \(i_a = r_2/(2r_3)\) (the identifier annulus_ratio) is the planetary gear ratio for the stopped sun wheel, \(r_s\) is the sprocket radius (the identifier r_sprocket), \(i_{fin}\) is the final drive ratio (the identifier final_ratio), \(i_{gb}\) is the gearbox ratio (the identifier gearbox_ratio). The identifier transmission_ratio corresponds to the parameter \(k_{main}\), track speed is measured in \(\text{km/h}\), and engine speed is measured in \(\text{rpm}\):

\[
\text{transmission_ratio} = r_{sprocket}/\text{gearbox_ratio}/\text{final_ratio} \cdot \text{annulus_ratio} \cdot 3.6\pi/30.
\]

The second expression is the relation between the track and engine speeds in a turn by stopped annulus

\[
v = \frac{i_s i_{steer}}{i_{fin}} \omega = k_{steer}\omega.
\]

Here \(i_s = r_1/(2r_3)\) (the identifier sun_ratio) is the planetary gear ratio for the stopped annulus, \(i_{steer}\) is the ratio of the simple gear connecting the secondary shaft and the sun wheel (the identifier steering_ratio). The identifier steer_ratio corresponds to the parameter \(k_{steer}\), track speed is measured in \(\text{km/h}\), and engine speed is measured in \(\text{rpm}\):

\[
\text{steer_ratio} = r_{sprocket}/\text{steering_ratio}/\text{final_ratio} \cdot \text{sun_ratio} \cdot 3.6\pi/30.
\]

Using these parameters, the ratio of speeds of inner \((v_i)\) and outer tracks \((v_o)\) in steering looks like

\[
v_i = \frac{(k_{main} - k_{steer})}{k_{main}} v_o.
\]

In the model, this ratio is presented by the identifier steer_speed_ratio.

18.1.6.7. Double differential steering system

A disadvantage of the "Maybach" steering system is the decrease of the TV speed in turning. A mechanism considered in this section allows turning without slowing the motion, Figure 18.131.
The body *Secondary shaft* is connected by gears the sun wheel shafts of two planetary mechanisms. The gears are modeled by special force elements *Steer gear left* and *Steer gear right*. The gear ratio is parameterized by the identifier *steering_ratio*. In a straight line motion of the TV, the secondary shaft is locked by a brake (a frictional torque in the joint *jSecondary shaft*), and the steering clutches *Steering clutch left/right* are disengaged.

For turning, the brake for the secondary shaft is released, and one of the steering clutches (the right one for the left turn) is engaged driving the secondary shaft in the necessary direction. So, the sun wheels of planetary gears are rotate in different directions increasing speed of the outer track and decreasing speed of the inner track.

The speed ratio of sprockets in turning for the inner \((v_l)\) and outer \((v_o)\) tracks looks like this:

\[
    v_l = \frac{k_{main} - k_{steer}}{k_{main} + k_{steer}} v_0.
\]
18.1.6.8. Double differential steering system (SU)

A modification of the "Maybach" double differential steering was implemented in the high-speed crawlers in USSR [4]. The mechanism in Figure 18.132 contains the same basic element as the "Maybach" system but some differences are important.

In a straight line motion, the steering clutches are engaged and the steering brakes are released, i.e. the sprocket rotation is summarized by planetary gears from two flows. In the gearbox the rotation of the secondary shaft drive the main shafts. Thus, the secondary shaft divides the energy on two, which are summarized by the planetary gears on the carries.

The mechanism allows the straight line motion on one power flow when the steering clutches are disengaged and steering brakes are applied.

For steering, the clutch on the side of the inner track is disengaged and the corresponding brake is released, i.e. the sun wheel is stopped and speed of the inner track decreases. The speed of TV in turning decreases like in the case of the "Maybach" steering system.
Steering brakes are described in joints $jSteering\ shaft\ left/right$, Figure 18.133. The speed ratio of sprockets in turning for the inner ($v_i$) and outer ($v_o$) tracks is

$$v_i = \frac{k_{\text{main}}}{k_{\text{main}} + k_{\text{steer}}} v_o.$$
18.1.6.9. Triple differential steering system

This modification of the double differential steering system (Sect. 18.1.6.7. "Double differential steering system", p. 18-102) allows replacing two steering clutches by two steering brakes, Figure 18.134.

In a straight line motion of TV, the steering brakes are released. For turning, the steering brake on the inner track side is applied to stop the sun wheel. Simultaneously, the steering differential increases the rotation speed of the sun wheel for the outer track.
18.1.6.10. Double differential steering system with hydrostatic drive (HSD)

Figure 18.135. Double differential steering system with HSD

Figure 18.136. Hydrostatic drive force element (HSD)
A hydrostatic drive allows turning TV with a continuously changing radius. The control parameter of steering is the normalized value of the pump valve specified by the identifier `steering_angle`, Figure 18.136. The control parameter is changed in the interval [-1,1].
18.2. Simulation of TV dynamics

In this section we do not consider general methods of simulation of multibody systems. We discuss some features of simulation of TV with UM. It is recommended to have a look at Chapter 4 of the manual “UM Simulation program” for studying the general methods of simulation.

18.2.1. Models of force interactions

Consider some features of force interaction of bodies in a model of TV.

18.2.1.1. Sprocket-pin interaction

Contact interactions of track pins with sprocket teeth transfers traction and brake torque to the track. A compliant contact model is used. Contact forces depend on penetration of pin and tooth profiles and produce two components, Figure 18.137: the normal force $N$ and the friction force $F$. The normal component is the linear function of the penetration and its derivative. Detailed description of mathematical model of the contact force can be found in Chapter 2 of the manual, Sect. Force elements| Contact forces | Points-Plane and Points-Z-surface types.

Contact stiffness and damping constants as well as coefficient of friction are specified by the user, Sect. 18.2.4.1. "Track contact parameters", p. 18-138.
Pin-sprocket contact forces are visualized in a special animation window, Figure 18.138. Use the Tools | Pin-sprocket contacts menu command to open the window.

Restrictive forces appear by the lateral shift of a track link relative to the sprocket as well as by relative rotations. Models of these forces are described in Sect. 18.2.1.5. "Restrictive force and moment", p. 18-117.

18.2.1.2. Track-ground interaction

The standard contact element of the Points–Z-surface type is internally used for description of interaction between a track link and the ground. One contact point is automatically assigned to each of the links. The point is located in the middle of the front edge of a lower bounding rec-
tangle of the link, Figure 18.139. Z – surface is designed taking into account irregularities under each of the track.

Two models of ground are implemented: a linear model without sinkage and a model of soil with sinkage.

**Remark.** Set of contact points of a link specifying its geometry is planned to be allowed in the nearest future.

### 18.2.1.2.1. Ground model without sinkage

A linear viscous-elastic model is used for the normal force

\[
N = -c_g \Delta - d_g \dot{\Delta},
\]

where \( \Delta, \dot{\Delta} \) is the depth of penetration of a contact point into the ground surface taking into account irregularities and its time derivative, \( c_g, d_g \) are stiffness and damping constants. The damping constant is computed according to the given value of the damping ratio \( \beta_g \) as

\[
d_g = 2\beta_g \sqrt{c_g m_t},
\]

where \( m_t \) is the mass of a track link.

Contact stiffness constants and damping ratio as well as coefficient of friction are specified by the user, Sect. 18.2.4.4.1. "Track contact parameters", p. 18-138.

This model can be used for modeling of ground without remarkable sinkage (concrete, asphalt and so on).

### 18.2.1.2.2. Bekker ground model

The Bekker model is implemented for ground taking into account sinkage processes [5], [1]

\[
p = \left( \frac{k_c}{b} + k_\varphi \right) z^n.
\]

Here \( p \) is the normal link-ground pressure; \( b \) is the minimal size on the contact patch \( b \) (length of a track link); \( n, k_c, k_\varphi \) are model parameters, \( z \) is the sinkage depth.

The Moor-Coulomb formula for the maximal shear strength is used in evaluation of friction forces

\[
\tau_{\text{max}} = c + p \tan \varphi,
\]

where \( c \) is the cohesion, \( p \) is the normal stress, \( \varphi \) is the angle of internal friction.

For evaluation of the current value of the shear strength, the following relation is usually applied [1]

\[
\tau(j, z) = (c + p \tan \varphi) \left( 1 - e^{j/K} \right),
\]

where \( j \) is the shear displacement of the link since the first contact with soil, and \( K \) is an empirical constant. The following simplified stress-displacement is implemented in UM
\[ \tau(j,z) = \begin{cases} \frac{c + p\tan\varphi}{K} & j < j^*, j^* = \frac{K\tau_{\text{max}}}{c + p\tan\varphi}. \end{cases} \] (18.2)

Figure 18.140. Example of track load force versus sinkage by loading and unloading/reloading processes

Eq. (18.1) is valid for the soil loading process. The linear model is implemented for the normal stress by unloading and reloading processes, figure 18.140

\[ p = p_u - k_u(z - z_u) \] (18.3)

Here \( p_u, z_u \) are the normal pressure and sinkage depth at the unloading start, \( k_u \) is the stiffness constant depending on \( z_u \). Usually the stiffness constant increases with the growth of the sinkage \( z_u \) due to the compaction of soil. The linear model is recommended [1]

\[ k_u = k_0 + A_u z_u \] (18.4)

which depends on two empirical constants \( k_0, A_u \). This formula fails for small sinkage, and an increased value is applied.

The normal and the friction forces are computes by multiplication of the corresponding stress and strength on the track area \( S \),

\[ N = pS, \quad F_{fr} = \tau S. \]

Thus, the soil model of (18.1) – (18.4) is specified by eight parameters

\[ n, k_c, k_{\varphi}, c, \varphi, K, k_0, A_u \]

which depend on the type and composition of the ground, moisture, temperature and so on. These parameters are assessed from field tests. Books [5], [1] contain over 50 examples of soil parameters, which can be used by simulations. Several pressure-sinkage plots from the UM database are presented in Figure 18.141.
Figure 18.141. Pressure versus sinkage
18.2.1.3. Rolling of wheel on track chain

The following forces are computed by rolling road wheels, idler and rollers on the track chain:

- normal forces;
- friction forces;
- restrictive forces in lateral direction;
- restrictive torques by misalignments.

18.2.1.4. Normal forces in wheel-track interaction

![Diagram of wheel penetration](image)

Figure 18.142. Penetration of a wheel into a plane

At the beginning we consider a model of interaction of a flexible wheel with a plane. The main idea: the normal contact force is proportional to the area $S$ of penetration of a ‘rigid wheel rim’ into the plane by vertical displacement of the wheel center $\delta$, Figure 18.142

$$ F = \kappa S. $$  \hfill (5)

where $\kappa$ is the constant of proportionality characterizing the wheel flexibility. The area $S$ can be expressed in terms of penetration $\delta$ or angle $\varphi$.

$$ S = \frac{2}{3} R^2 \varphi^3, \quad \varphi = \frac{2\delta}{R}. $$  \hfill (6)

Substitution of Eq. (6) into Eq. (5) gives the dependence of the force on the penetration

$$ F = \frac{2}{3} \kappa R^2 \varphi^3 = \frac{4}{3} \kappa \sqrt{2} \delta^{3/2}. $$

Note that the exponent factors in this formula and in the Hertz formula for contact of two semispaces are the same, which confirms the correctness of the above assumption.

Let us obtain the dependence of the stiffness factor on the penetration
The derived formulas allow a simple identification of the model parameters by stiffness \( c \) for the given load \( P \) or by the deflection \( \delta_0 \) for the load \( P \)

\[ \delta_0 = \frac{3 P}{2 c}, \kappa = \frac{1}{2} \sqrt{\frac{c^3}{3PR}} \] (7)

The following formulas can be useful as well

\[ F = P(\delta/\delta_0)^{3/2}, \quad c(\delta) = \frac{dF}{d\delta} = c(\delta/\delta_0)^{1/2}. \]

Now the obtained relations can be generalized for a contact of a wheel with a polyline corresponding to the track chain.

Let us accept the following assumption: the force is perpendicular to a separate section of the polyline, i.e. to a track link, and proportional to the penetration area under the section.

The following formula can be derived in the local system of coordinates of a track link, Figure 18.143

\[ x^\pm = x_c \pm R\sin\varphi. \]

Contact conditions are

\[ \{x^- < \frac{1}{2}\} \cap \{x^+ > -\frac{1}{2}\}. \]

It is better to compute the force and moment in SC, which origin is located exactly under the center of the circle.
Using the circle equation, the formula for penetration versus longitudinal coordinate can be obtained

\[ dz = \left| R - \delta - \sqrt{R^2 - x^2} \right| \approx \left| R - \delta - R \left( 1 - \frac{x^2}{2R^2} \right) \right| = \delta - \frac{x^2}{2R}. \]

The force is computed as

\[ dF = \kappa dx dz, \]

\[ F = \kappa \int_{x_1}^{x_2} \left( \delta - \frac{x^2}{2R} \right) dx = \kappa \left( \delta x - \frac{x^3}{6R} \right) \vline_{x_1}^{x_2}. \]

Here the limits of the integration interval are

\[ x_1 = \max \left\{ -b, -\frac{l}{2} - x_c \right\}, \quad x_2 = \min \left\{ b, \frac{l}{2} - x_c \right\}, \]

\[ b = \sqrt{2R\delta}. \]

Test: by \(-x_1 = x_2 = b\) the above formula for the plane takes place.

To get the application point for the resultant force, the moment relative to the origin of SC must be computed

\[ dM = x dx dz = \kappa x dx dz \]

\[ M = \kappa \int_{x_1}^{x_2} \left( \delta x - \frac{x^3}{2R} \right) dx = \kappa \left( \frac{\delta x^2}{2} - \frac{x^4}{8R} \right) \vline_{x_1}^{x_2}. \]

Now, the coordinate for the resultant force is

\[ x^* = \frac{M}{F} + x_c. \]
18.2.1.5. Restrictive force and moment

To fix the lateral shift of the track relative to the wheels and rotation about the longitudinal axis, a force and a moment applied to links are introduced

\[ F_y = -c_y \Delta y - d_y \Delta \dot{y}, \]
\[ M_x = -c_{ax} \alpha_x - d_{ax} \omega_x. \]  \( \text{(8)} \)

Here \( \Delta y \) is the lateral shift of the link relative to the wheel, \( \alpha_x, \omega_x \) are the relative angle and angular velocity of the link rotation about the longitudinal direction, Figure 18.145; \( c_y, d_y \) are the stiffness and damping constants in the lateral direction, \( c_{ax}, d_{ax} \) are the angular stiffness and damping constants.

Conditions for initiation of the force and moment is the inequality

\[ TC < R, \]

corresponding to the contact between the link tooth and the wheel slot; here \( T \) is the top point on the tooth specified by the tooth height \( h_t \), Figure 18.145, \( R \) is the wheel radius.

The user must set numerical values for the following parameters: stiffness constant \( c_y \), damping ratio \( \beta_y \), tooth height \( h_t \) (see Sect. 18.2.4.1. "Track contact parameters", p. 18-138).

Other parameters are computed according to the formulas

\[ d_y = 2\beta_y \sqrt{m_t c_y c_{ax}} \]
\[ c_{ax} = c_y l^2, \]
\[ d_{ax} = 2\beta_y \sqrt{J_{lx} c_{ax}} \]

where \( m_t, l, J_{lx} \) is the track link mass, length and moment of inertia relative to the longitudinal axis.

18.2.1.6. Force for hull locking in horizontal plane

Some tests with the TV model require fixing TV hull in longitudinal and lateral direction as well as by rotation about the vertical axis. In these tests, the linear spring-damper force in the horizontal plane and a torque are applied to the hull.
Here $\Delta x, \Delta y$ are deviations of the hull center of gravity in the horizontal plane, $\gamma$ is the hull rotation about the vertical axis, $c_{xy}, d_{xy}$ are the spring and damper rates, $\beta_{xy}$ is the damping ratio, $m_h$ is the hull mass.

Stiffness constant $c_{yx}$ and damping ratio $\beta_{xy}$ are specified by the user, Sect. 18.2.4.4.1. "Track contact parameters", p. 18-138.

18.2.1.7. Evaluation of stiffness constant in wheel-track contacts

Two methods can be used for evaluation of road wheel-track contact parameters. According to the first one, the deflection of the wheel center $\delta_0$ under the static load $P$ is used. Value of the stiffness constant is computed by Eq. (7)

$$c = \frac{3 \ P}{2 \ \delta_0}.$$

According to the second method, the user must know the stiffness $c$ under the load $P$ directly.

For contacts of the track with idler and rollers, the same values of stiffness parameters can be used because of lower influence of these contacts on dynamics of the TV.

Contact stiffness and damping ratios are specified by the user, Sect. 18.2.4.4.1. "Track contact parameters", p. 18-138.
18.2.2. Controlled motion of TV

18.2.2.1. General information about controlled motion of TV

We consider a systematical change of speed or the longitudinal control as well as turning control.

In a case of a simplified model of TV without the driveline, both types of control are realized by the direct support of a desired value of angular velocities of the sprockets. Let \( v_l, v_r \) be the current values of the circular speed of the left and right sprocket, which are computed by the formula \( v = \omega R_s \), where \( \omega \) is the angular velocity of the sprocket, and \( R_s \) is the sprocket radius on the pin centers. Let \( V_l, V_r \) be the desired values of these speeds. The control torque is applied to the sprockets from the TV hull proportionally to the speed differences

\[
M_l = -k(\omega_l R_s - V_l), \quad M_r = -k(\omega_r R_s - V_r),
\]

where \( k \) is the amplification.

When the TV moves on a straight section of road, the desired speeds \( V_l, V_r \) are equal and specified by the user as a plot of the longitudinal speed versus the time or distance (TV travel)

\[
V_l = V_r = \begin{cases} V(t), & t - \text{time}, \\ V(s), & s - \text{distance}. \end{cases}
\]

A difference of the right and left sprocket speeds is implemented for the TV turning

\[
\Delta V = V_r - V_l.
\]

A positive difference corresponds to the left turn, while a negative related to the right one.

Two methods are implemented to turn TV, which we will designate as a symmetric turning and a unilateral one. In the case of a symmetric turn, the sprocket speed increases on \( \frac{\Delta V}{2} \) for the outer track and decreases on the same value for the inner track, i.e.

\[
V_l = V - \Delta V/2, \quad V_r = V + \Delta V/2,
\]

where \( V \) is the desired longitudinal speed. Such the control corresponds to a differential gear as a turning mechanism.

In the case of a unilateral turn, the sprocket speed is constant for the outer track and decreases on \( \Delta V \) for the inner one,

\[
V_l = \begin{cases} V - \Delta V, & \Delta V > 0, \\ V, & \Delta V < 0, \end{cases} \quad V_r = \begin{cases} V, & \Delta V > 0, \\ V + \Delta V, & \Delta V < 0. \end{cases}
\]

This case corresponds e.g. to a simplified model of a side clutch.

The value \( \Delta V \) specifies the turning radius and can be set by the user as an explicit function of the time or the distance, which corresponds to an open loop turning control, Sect. 18.2.4.3. "Tools tab: setting speed history", p. 18-136, Sect. 18.2.4.5.6.2. "Test: open loop steering", p. 18-163. In another case this value is evaluated by the driver model and allows automatic motion along given routes, Sect. 18.2.4.5.6.3. "Test with driver", p. 18-164.
**18.2.2.2. Driver model**

Consider the driver model implemented in UM. Let the desired path (route) is given, Figure 18.146. The internal ‘driver’ must follow it. The control with the closed loop or the driver model is as follows: at the moment $t$ the driver assesses the deviation $\Delta y(t)$ from the route a point located straight ahead on a preview distance $L_p = T_p v_x$. Here $T_p v_x$ are the preview time, specified by the user, and the vehicle speed. The control is

$$\Delta V = K \Delta y(t - t_d),$$

where $K$ is the gain, $t_d$ is the reaction time delay.

**Table 18.21**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Comments</th>
<th>Recommended interval of values</th>
<th>Default value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_p$</td>
<td>Preview time</td>
<td>1-2s</td>
<td>1s</td>
</tr>
<tr>
<td>$t_d$</td>
<td>Reaction time delay</td>
<td>&gt;0.1s</td>
<td>0.1s</td>
</tr>
<tr>
<td>$K$</td>
<td>Gain</td>
<td>3-6</td>
<td>4</td>
</tr>
</tbody>
</table>

Numeric values of the control parameters depend on the speed, route, and TV, Table 18.21. The user should run several simulations with different values of the parameters to get a stable and reliable control.
18.2.2.3. Geometry of controlled motion of TV

18.2.2.3.1. Straight motion

The driver model is not used for this type of motion, because circular speeds of sprockets are equal. Vertical irregularities and obstacles can be assigned.

18.2.2.3.2. Plane curve

The user specifies a plane curve as a desired path for the TV motion with the driver model. Vertical irregularities can be assigned.

A curve editor is used for development of paths. The Tools | Create macrogeometry... menu command calls the window, Figure 18.149. The desired path is created in the curve editor by the button.
18.2.2.3.3. Testing area

A testing area (TA) is a surface with a set of testing obstacles. The TV model overcomes the obstacles following to a route defined by the user. The image of TA is created in one of the CAD programs and imported to UM format in the standard manner. The image must contain one GO and should be saved in a *.img file. The UM database of TA contains two areas:

- `{UM Data}\Caterpillar\TestingArea\TestingArea.img` (Figure 18.150);
- `{UM Data}\Caterpillar\TestingArea\SandPit.img`.

The user creates a set of routes for a TA. Motion or TV along a route with a definite variable speed is controlled by the driver model. Micro irregularities can be taken into account alone with the obstacles.
18.2.3. Classification of dynamic tests

Simulation of TV dynamics in UM is based on a system of tests. Here is the current list of available tests:

1. equilibrium,
2. track tension,
3. tension by joint preload,
4. computation of initial velocities,
5. vertical harmonic loading,
6. straight motion,
7. open loop steering,
8. test with driver.

The tests can be divided into two groups: auxiliary (1-5) and main test (6-8). Auxiliary tests are used for computation of initial state of TV and for preparing the main tests. The main tests are used for analysis of dynamic properties of TV.

TV is fixed in longitudinal direction in tests 1-5. Tests 6-8 allow evaluation of dynamic performances by motion taking into account ground profile and irregularities.

It is recommended to run the tests in the above sequence.

18.2.4. Preparing TV for simulation

Before start the tests, the user must do definite steps to prepare the TV model. With this purpose, the Tracked vehicle tab of the object simulation inspector is used.

![Object simulation inspector](image18.151.jpg)

Figure 18.151. Object simulation inspector

Load the TV model in UMSimul program. Call the simulation inspector by the Analysis | Simulation menu command, Figure 18.151. The button on the tool panel as well as the F9 key can be used as well.

**Remark.** The inspector contains several useful general purpose tabs: Identifiers, Solver, Initial conditions, Tools, Object variables, see Chapter 4 “UM Simulation program”, Sect. Integration of equations of motion (single mode) | Preparing for integration.

Consider a list of main control elements on the Tracked vehicle tab.
**Button** is used for saving the TV parameters and options specified by the user on the tab, file with configuration of TV is *.tvc.

**Button** reads parameters of TV from a previously created configuration file *.tvc.

**Button** shows current irregularities for the left and right tracks in a graphic window, Sect. 18.2.4.1.2.4. "Examples of irregularities", p. 18-127. The same action is assigned to the button on the main tool panel.

![Menu of quick access](image)

**Figure 18.152. Menu of quick access**

**Button** organizes a quick access to different tabs and parameters, Figure 18.152.

The **Options** tab: setting some parameters of TV and operation conditions such as track tension parameter, ground irregularities, assigning a testing area, etc., Sect. 18.2.4.1. "Options tab", p. 18-125.

The **Resistance** tab allows specification of aerodynamic drag, Sect. 18.2.4.2. "Resistance tab", p. 18-135.

The **Tools** tab: creation of TV speed dependences on time or distance, Sect. 18.2.4.3. "Tools tab: setting speed history", p. 18-136.

The **Identification** tab: specification of auxiliary parameters for dynamic tests such as contact parameters, blocking force parameters, specification of identifiers for sprocket torques, soil parameters, Sect. 0.

The **Tests** tab is used for selection of a current test and definition of its parameters.
18.2.4.1. Options tab

TV options tab contains three elements:
- General options,
- Irregularities for each of the track,
- Macrogeometry parameters.

18.2.4.1.1. General options

The General tab allows the user to set the following parameters, Figure 18.154.

1. Initial rotation angles of sprockets.
2. A body in the model as the hull of TV. Program assigns the body with the maximal mass, but the user may correct this assignment if necessary.
3. Elongation of the tension device and/or preload in the track link joints (bushings) to get the desired tension of tracks. Numeric values of these parameters are evaluated in the tests Track tension (Sect. 18.2.4.5.2. "Test: track tension", p. 18-146) and Tension by preload (Sect. 18.2.4.5.3. "Test: tension by preload", p. 18-151).
18.2.4.1.2. Irregularities

In the main tests, Sect. 18.2.3. "Classification of dynamic tests", p. 18-123, irregularities can be assigned both for the left and right tracks, Figure 18.155.

18.2.4.1.2.1. File with irregularities

Text files *.irr contain vertical ground irregularities for the left or right track of TV.

*File format.* File with irregularities contains two columns. The first column contains the longitudinal coordinate (distance) in meters starting from 0. The second one corresponds to the vertical coordinates of the ground in meters. Example:

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>-0.00540956</td>
<td></td>
</tr>
<tr>
<td>0.1</td>
<td>-0.00553727</td>
<td></td>
</tr>
<tr>
<td>0.2</td>
<td>-0.00564776</td>
<td></td>
</tr>
<tr>
<td>0.3</td>
<td>-0.00574484</td>
<td></td>
</tr>
<tr>
<td>0.4</td>
<td>-0.00583378</td>
<td></td>
</tr>
<tr>
<td>0.5</td>
<td>-0.00592044</td>
<td></td>
</tr>
<tr>
<td>0.6</td>
<td>-0.00601059</td>
<td></td>
</tr>
<tr>
<td>0.7</td>
<td>-0.00610933</td>
<td></td>
</tr>
</tbody>
</table>

*Creating irregularity files.* A special tool can be used for creating irregularities. This tool was initially developed for description of rail irregularities. Use the Tools | Create irregularities… or the button on the tool panel.

Detailed information about the tool can be found in the user’s manual, Chapter 12, Sect. Generation of irregularity files, and Chapter 8, Sect. Creation of files with irregularities.

*File locations.* Standard irregularity files are located in the directory {UM Data}\Caterpillar\Irregularities.

It is recommended to save user’s files either in this directory or in the directory of the modeled TV.

*Assignment of irregularity files.* Click the button to select a file, Figure 18.155a.
18.2.4.1.2.2. Harmonic irregularities

In this case, the vertical ground profile is computed by the formula

$$z = a \sin \frac{2\pi}{L} (x - x_0),$$

where $a$ is the amplitude, $L$ is the wave length (a period), $x$ is the longitudinal coordinate, $x_0$ is the phase shift for the right track.

18.2.4.1.2.3. Smooth run on irregularities by start

To avoid a jump in forces by run on irregularities at the initial stage of motion, the irregularities are set to zero at the first five meters of the running distance, and a smoothing is used.

In the case of harmonic irregularities, the smoothing is made from 5 to 15 meters by a square function with the growth from 0 to 1, i.e. the function is multiplied by the factor $(x-5)^2/100$.

In the case of file irregularities, the smoothing is made from 5 to 10 meters by a linear function, i.e. the irregularity is multiplied by the factor $(x-5)/5$. For example, consider a file irregularity of the constant height 100mm. The smoothed irregularity, which is used in simulations, is shown in Figure 18.156.

![Smoothed ground profile](image)

Figure 18.156. Smoothed ground profile

18.2.4.1.2.4. Examples of irregularities

After entering irregularity parameters, the plot can be obtained by the button. Figure 18.157 shows an example of a sinusoidal ground profile for the parameter values $A=100\text{mm}$, $L=8\text{m}$, $x_0=2\text{m}$.
An example of the ground profile for simulation of TV jump is shown in Figure 18.158.

18.2.4.1.2.5. Visualization of road

By straight motion of TV, strips of road with irregularities are drawn for the left and right tracks. Figure 18.159 shows animation windows with ground profiles corresponding to irregularities in Figure 18.157, Figure 18.158.

Width and color of the strips can be set in the Macrogeometry tab, Sect. 18.2.4.1.2.5. "Visualization of road", p. 18-128.
Figure 18.159. Examples of irregularities
18.2.4.1.3. Parameters of macrogeometry

18.2.4.1.3.1. Testing area

Assignment of testing area (TA)

Use the button in Figure 18.167 to select a file *.img with the TA image.

Creating and editing of routes

A route is a curve created by the user on a TA. The TV model follows the assigned route on the TA under control of the driver model, Sect. 18.2.2.2. "Driver model", p. 18-120, Sect. 18.2.2.3.3. "Testing area", p. 18-122.

The following tools are available of the tab.

- Adding a new route to the list of routes
- Deleting a route from the list
Adding a new route and start the mode for the visual creating a route by the mouse

After click on this button, the animation window with the TA image appears. The user creates here a sequence of markers (key points) on the route, Figure 18.161. The following recommendations are important.

- The first and the second markers should be located on a horizontal part of the TA. These points set the initial position of the TV on the TA by a shift and rotation of the TA so that the origin of SC0 coincides with the first marker, and the X-axis passes through the second one, Figure 18.162.

![Figure 18.162. Examples of initial positions of TV for different routes](image)

- Markers a set in positions corresponding to changes of directions of motion (start and end points of the TV turnings) as well as in positions where it is planned to change the TV speed, Figure 18.163.

- After end of selection of the markers, close the window and confirm the acceptance of data input.

![Figure 18.163. Markers specify the interval of the braking process](image)
**Correcting routes in the curve editor**

After the click on this button, the curve editor appears containing all the routes, Figure 18.164. It is necessary to check one route curve, which is to be modified. Uncheck all other curves.

In the editor, the user can
- correct coordinates of points;
- add and delete any number of points;
- smooth some section by circles and splines, Figure 18.165.

Detailed information on the curve editor can be found in Chapter 3 of the user’s manual, Sect. Curve editor.

![Curve editor](image)

**Figure 18.164.** Routes in the curve editor. All routes except the checked one, are hidden

![Route after editing](image)

**Figure 18.165.** Route after editing

**View of route in animation window**

Select a route in the list and click this button. An animation window with TA image and the route appears. If the mouse cursor points to a route marker, coordinates of the marker and the *distance* S to it along the route can be found in the window status bar, Figure 18.166.
Save the route list to file

The routes are saved in a text file *.rt; name of the file is the name of the TA. The file is stored in the same directory as the TA file. For instance, the route file for the TA

\{UM Data\}\Caterpillar\TestingArea\TestingArea.img

will be saved as

\{UM Data\}\Caterpillar\TestingArea\TestingArea.rt.
18.2.4.1.3.2. Parameters of the road image

On the Macrogeometry tab, the user can change parameters of visualization of the road strips, Figure 18.167, Sect. 18.2.4.1.2.5. "Visualization of road", p. 18-128:

- strip width;
- discretization step in longitudinal direction;
- color.

For the tests with driver by motion on 2D curve:

- road width.

For the test with driver:

- line color for the route, Figure 18.162.

![Figure 18.167. Parameters of road image](image-url)
Aerodynamic drag is specified by three parameters:
- air density $\rho$,
- drag coefficient $c_w$,
- area of TV projection on the plane perpendicular the TV axis ($A$).

The force is computed by the formula

$$W = c_w A (\rho/2) v^2,$$

where $v$ is the TV speed.
18.2.4.3. Tools tab: setting speed history

The **Tools** tab is used for creation of speed history files

- desired track speed difference $\Delta V$ for open loop steering test,
- desired longitudinal speed $V$ for tests with longitudinal motion.

The speed curve can be a function of either time or distance.

To create the speed history, call the curve editor by the **button and define a curve as a sequence of points. An example of a speed vs. time curve is shown in Figure 18.170. Here the speed increases with a constant acceleration from 0 to 10 m/s, and then the speed is constant.

**Remark.** By specifying the speed versus distance curve, the initial speed cannot be zero.
18.2.4.4. Identification tab

The following parameters are specified on the Identification tab (Figure 18.171):

- track contact parameters,
- locking parameters for hull horizontal motion,
- identification of drive torques applied to sprockets,
- terrain parameters.

![Identification of TV model parameters](image)
### 18.2.4.4.1. Track contact parameters

#### Table 18.22

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Default value</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ground stiffness (N/m)</td>
<td>1.0e8</td>
<td>Sect. 18.2.1.2. &quot;Track-ground interaction&quot;, p. 18-110.</td>
</tr>
<tr>
<td>Ground damping ratio</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Coefficient of ground friction</td>
<td>0.3</td>
<td></td>
</tr>
<tr>
<td>Sprocket stiffness (N/m)</td>
<td>1.0e7</td>
<td>Sect. 18.2.1.1. &quot;Sprocket-pin interaction&quot;, p. 18-109.</td>
</tr>
<tr>
<td>Sprocket damping ratio</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Coefficient of sprocket friction</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Road wheel stiffness (N/m)</td>
<td>1.0e6</td>
<td>Sect. 18.2.1.7. &quot;Evaluation of stiffness constant in wheel-track contacts&quot;, p. 18-118.</td>
</tr>
<tr>
<td>Road wheel damping ratio</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Coefficient of wheel friction</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>Idler stiffness (N/m)</td>
<td>1.0e6</td>
<td></td>
</tr>
<tr>
<td>Idler damping ratio</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Roller stiffness (N/m)</td>
<td>1.0e6</td>
<td></td>
</tr>
<tr>
<td>Roller damping ratio</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Lateral stiffness (N/m)</td>
<td>1.0e8</td>
<td>Sect. 18.2.1.5. &quot;Restrictive force and moment&quot;, p. 18-117.</td>
</tr>
<tr>
<td>Lateral damping ratio</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>Guide tooth height (mm)</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>Max. track Z travel (mm)</td>
<td>100000</td>
<td>Maximal vertical travel of track links relative to the hull. Ignored if value is greater than 10000. For instance, the contact is ignored for the default parameter value</td>
</tr>
</tbody>
</table>

Parameters of contact of track with ground and wheels are set in the table, Figure 18.171, Table 18.22, Sect. 18.2.1. "Models of force interactions", p. 18-109.

**Remark.** Damping ratios $\beta$ in Table 18.22 are used for computation of damping constants $d$ by the stiffness constant $c$ and body mass $m$ as

$$d = 2\beta \sqrt{mc}$$

As a rule the smallest mass $m$ of the contacting bodies is used in this expression.
18.2.4.4.2. Hull locking parameters

Locking is used in some tests for fixing the hull motion in the horizontal plane. Stiffness constant as well as the damping ratio are set in the table, Sect. 18.2.1.6. "Force for hull locking in horizontal plane", p. 18-117.
18.2.4.4.3. Traction torques

Identifiers of traction torques must be selected in the table, Sect. 18.1.1.4.3.4. "Template of sprocket", p. 18-51, Table 18.14. If the standard identifier "traction_torque" is used, this assignment is done automatically.

If the user renamed the identifier in the sprocket template, he must select the corresponding identifiers from the list after the double click on the table cell in Figure 18.173.

![Figure 18.173. Identifiers of traction torques](image-url)
18.2.4.4.4. Terrain parameters

In the case of the main tests, ground with sinkage model can be applied, Sect. 18.2.1.2.2. "Bekker ground model", p. 18-111. Parameters can be set directly into the table in Figure 18.174, or assigned from the database with the help of the drop-down list.
Before run the simulation with a TV model, the user must select one of the available tests from the list in Figure 18.175 and initialize necessary parameters related to the test.

Two types of parameters can be related to a test (Parameters tab in Figure 18.175):

- **Identifiers**: the initialization in this case consists in assignment of identifiers from the TV model; it is recommended to use the standard identifier names by development of TV models: in this case the assignment will be done automatically;

- **Numeric parameters**: the user set desired values of these parameters.

A list of standard test variables is available for the most of the tests on the Variables tab in Figure 18.175. The user can get plots of these variables if he drags them into a graphic window before simulation.
18.2.4.5.1. Test: Equilibrium

Test objective.

This is an auxiliary test intended for finding coordinates of bodies in the TV equilibrium state. The test is necessary because positions of bodies in the TV model after its development in the UM Input are specified approximately, Figure 18.177. Thus, intensive transient processes take place by the start of simulation. The test is used to remove these transients. As a rule, this is the first test with a new TV model or after change of inertia or suspension parameters.

Remark. Ground friction is automatically set to zero during this test.

Initialization of test parameters

There are no parameters in this test.

Figure 18.176. Standard variable of equilibrium test

Figure 18.177. Positions of track links before and after the equilibrium test

Figure 18.178. Decrease of kinetic energy of TV
Test variables.

Kinetic energy is the standard variable of the test. User stops the test when the energy value becomes small enough, Figure 18.178.

Plots of road wheel loads are useful during the test as well, Figure 18.179. These variables are available in the **Wizard of variables**, Sect. 18.2.6. *“List of special variables for tracked vehicles”*, p. 18-167.

![Figure 18.179. Road wheel loads](image)

Test results.

To save the test results it is necessary
• to call the pause mode by the button in the Process parameters window or by the ESC key;
• to save body positions in a *.xv file by the Save button, Figure 18.180;
• to break the simulation by the Interrupt button;
• in the Object simulation inspector
  - open the Initial conditions tab;
  - read the just saved file by the button;
  - set zero values for velocities by the button;
  - save the final values of coordinates in a file by the button.

  The created file is used in some other tests for setting initial positions of bodies.

**Remark.** The Track tension or Tension by joint preload tests can be used instead of the Equilibrium test.
18.2.4.5.2. Test: track tension

**Test objective.**

This is an auxiliary test, which is used for setting a desired track tension in case of track links with *rigid joints*. Change in the track tension is achieved by increase of length of a tension force element, Sect. 18.1.1.4.2. "Idler and tension device", p. 18-31.

**Remark.** Ground friction is automatically set to zero during this test.

**Initialization of test parameters.**

*Identifiers:* identifiers parameterizing elongation of the tension force element for the left and right tracks is to be assigned. The default identifier is *dl_tension_rod*. If the user renamed the identifier in the idler template, he must select the corresponding identifiers from the list after the double click on the corresponding table cell (Figure 18.181, the second column in the table).
Numeric parameters set the process of the tension rod elongation:

- **TStart (s)**: moment of elongation start;
- **DLStart (mm)**: initial value of elongation;
- **DLFinish (mm)**: final value of elongation;
- **V (mm/s)**: elongation velocity.

An example of the elongation process is shown in Figure 18.182 for the following parameter values:

- **TStart=1**;
- **DLStart=0**;
- **DLFinish=50**;
- **V=5**.

**Test variables.**
The list of standard test variables includes the value of elongation as well as an average track tensions $S$, Figure 18.181

$$S = \frac{\sum_{i=1}^{n} S_i}{n},$$

where $S_i$ is the reaction force in track joint $i$, $n$ is the number of links.
Chapter 18. Tracked vehicles

Test results.

The main result of the test is the plot of tension force vs. elongation, Figure 18.183. To get this plot, the following steps are necessary before start of the simulation:

- open new graphic window;
- drag two variables from the table in Figure 18.181 by the mouse into the window: elongation and tension;

Figure 18.183. Tension vs. elongation

Figure 18.184. Elongation must be laid off as abscissa
• lay off the elongation as abscissa: select the variable in the list of graphic window, call the context menu by the right mouse button and select the menu command, Figure 18.184.

After the simulation,
• evaluate the elongation $l^*$ by the necessary tension, Figure 18.183;
• replace the maximal elongation in the table of numeric test parameters DLFinish by the value $l^*$ (Figure 18.181) and run simulation again;
• following the Sect.
• Test: Equilibrium, save coordinates in a file and use these values as initial conditions for other tests;
• finally, set the elongation \( l^* \) as the standard one in the box **Elongation of tension rod**, the **Tracked vehicle | Options | General** tab, Sect. 18.2.4.1.1. "General options", p. 18-125, Figure 18.154.

**Remark.** The test must be repeated every time when the tension value is changed or if parameter values exerting the tension like suspension stiffness are changed.
18.2.4.5.3. Test: tension by preload

**Test objective.**

This is an auxiliary test, which is used for setting a desired track tension in case of track links with *flexible and parallel joints*. The desired track tension is achieved by change of preload force in joint, Sect. 18.1.1.4.2. "Idler and tension device", p. 18-31.

**Remark.** Ground friction is automatically set to zero during this test.

**Initialization of test parameters.**

*Identifiers*: identifiers parameterizing the preload force in track link joints for the left and right tracks is to be assigned. The default identifier is *track_tension*. If the user renamed the identifier in the idler template, he must select the corresponding identifiers from the list after the double click on the corresponding table cell (Figure 18.185, the second column in the table).
Numeric parameters set the process of increase the preload value:
TStart (s): moment of preload increase start;
PStart (kN): initial value of preload;
PFinish (kN): final value of preload;
PV (kN/s): preload rate.

An example of dependence of the preload on time is shown in Figure 18.186 for the parameter values:

\[ T_{\text{Start}}=0; \ P_{\text{Start}}=0; \ P_{\text{Finish}}=35; \ P_{\text{V}}=6. \]

Test variables.
The list of standard test variables includes the value of preload as well as an average track tensions \( S \), Figure 18.181

\[ S = \frac{\sum_{i=1}^{n} S_i}{n} \]

where \( S_i \) is the force in track joint \( i \), \( n \) is the number of joints.
Test results.

The main result of the test is the plot of tension force vs. preload, Figure 18.187. To get this plot, the following steps are necessary before start of the simulation:

- open new graphic window;
- drag two variables from the table in Figure 18.185 by the mouse into the window: preload and tension;

Figure 18.187. Example: tension vs. preload

Figure 18.188. Preload must be laid off as abscissa
• lay off the preload as abscissa: select the variable in the list of graphic window, call the context menu by the right mouse button and select the menu command, Figure 18.188.

After the simulation,
• evaluate the preload \( P^* \) by the necessary tension, Figure 18.187;
• replace the maximal preload in the table of numeric test parameters PFinish by the value \( P^* \) (Figure 18.181) and run simulation again;
• following the Sect.
Test: Equilibrium, save coordinates in a file and use these values as initial conditions for other tests;

finally, set the preload value $P^*$ as the standard one in the box **Preload in joint**, the **Tracked vehicle | Options | General** tab, Sect. 18.2.4.1.1. "General options", p. 18-125, Figure 18.154.

**Remark.** The test must be repeated every time when the tension value is changed or if parameter values exerting the tension like suspension stiffness are changed.
18.2.4.5.4. Test: Vertical harmonic loading

**Test objectives.**

This is an auxiliary test for evaluation of stiffness characteristics of the suspension system as a plot of force vs. vertical movement. During the test, a harmonic force $F$ is applied to the center of gravity of the TV hull

$$F = F_0(1 - \cos(2\pi ft))/2,$$

where $F_0$ is the maximal force value, $f$ is the excitation frequency in Hz. The force is directed downwards.

Initialization of test parameters.

The user sets two numeric parameters: the maximal force $F_0$ and the frequency $f$. Figure 18.189.

Test variables.

The list of standard variables includes the excitation force value (kN) and the vertical displacement of the hull center of gravity (mm).

Test results.

![Graph showing test results](image)

0.2 Hz
Figure 18.190. Force versus displacement for different values of frequency

The main result is the plot of force versus displacement, Figure 18.190. The following steps are required for getting the plot:

- open a new graphic window;
- drag both variable in the window from the list in Figure 18.189;
- lay off the hull movement as abscissa.
18.2.4.5.5. Test: Computation of initial velocities

Test objectives.

This is an auxiliary test for creation of a file of initial conditions, which is used for computation of initial velocities of bodies in the case of an arbitrary initial speed of TV.

The test runs as follows. At start of the test the TV does not move. Then the ground is moved backwards with a constant acceleration, and the hull is locked in the horizontal plane. As a result, the tracks move with acceleration. After reaching a definite speed, the ground moves uniformly. After finish the test, the user saves positions and velocities of bodies in a file [numeric value of speed*10].tvv, e.g., 50.tvv corresponds to the test results with the target speed 5 m/s.

The created file is used by the main tests, where the user can set any initial speed of TV. By the start of such a test, UM finds the *.tvv file with the nearest value of speed and computes velocities of all the bodies using the saved data. Usually it is enough to create only one *.tvv file with an average speed, and UM correctly specifies velocities of bodies for any initial speed of TV.
**Initialization of test parameters.**

The list of test parameters includes two numeric constants: the target speed of TV and the time interval for the uniform acceleration.

**Test variables.**

Two standard variables are the circular velocities of sprockets

\[ v = \omega R_s, \]

where \( \omega, R_s \) are the angular velocity of a sprocket and the sprocket radius on the pin centers. An example is shown in Figure 18.192.
18.2.4.5.6. Tests with longitudinal motion of TV

There are three tests with longitudinal motion of TV:

- straight motion,
- open loop steering,
- test with driver.

Consider common parameters of these tests.

Figure 18.193. Value of amplification

1. **Amplification** $k$ (Figure 18.193) in the control of the circular speed of sprockets, Sect. 18.2.2.1. "General information about controlled motion of TV", p. 18-119.

Figure 18.194. Test options

2. Option **Take into account irregularities** (Figure 18.194), Sect. 18.2.4.1.2. "Irregularities", p. 18-126.

3. **Type of soil** allows setting either linear model of the ground (Sect. 18.2.1.2.1. "Ground model without sinkage", p. 18-111), or a model with sinkage, Sect. 18.2.1.2.2. "Bekker ground model", p. 18-111. In the first case, the ground stiffness, damping ratio and coefficient of friction are specified in the table of contact parameters, Sect. 18.2.4.4.1. "Track contact parameters", p. 18-138. In the second case the parameters are set in the table of terrain parameters, Sect. 18.2.4.4.4. "Terrain parameters", p. 18-141.

4. **Longitudinal motion mode** includes three modes of the TV speed control:
   - Neutral: speed control is not used;
   - $v=$const: motion with a constant speed;
   - $v(t)/v(s)$: dependence of speed on time or distance is supported.
In the case of two first modes, the initial speed is assigned to the identifier $v_0$ on the **Identifier** tab of the inspector, Figure 18.195.

In the third case the speed vs. time\distance history must be assigned, Sect. 18.2.4.3. "Tools tab: setting speed history", p. 18-136. The file is assigned by the $\mathbb{E}$ button in Figure 18.196.
18.2.4.5.6.1. Test: straight motion

Test objectives.
This is one of the main tests, which allows estimating dynamic performances of a TV. In the test, a straight motion of a TV is considered. Three modes of TV speed are implemented. Irregularities of the ground can be taken into account.

Test parameters are described in Sect. 18.2.4.5.6. "Tests with longitudinal motion of TV", p. 18-160.

The road irregularities are set on the Options | Irregularities tab, Sect. 18.2.4.1.2. "Irregularities", p. 18-126.

Test results.
All standard kinematic and dynamic variables can be considered as test results. Use the Wizard of variables for creating the variables, Sect. 18.2.6. "List of special variables for tracked vehicles", p. 18-167.
18.2.4.5.6.2. Test: open loop steering

In addition to the standard parameters for tests with longitudinal motion, the test requires the following data:

- type of turning mechanism, Sect. 18.2.2.1. "General information about controlled motion of TV", p. 18-119.
- control: sprocket speed difference $\Delta V$ for turning the TV, Sect. 18.2.2.1. "General information about controlled motion of TV", p. 18-119, 0; the preliminary created file is assigned by the button, Figure 18.197, Figure 18.198.

Figure 18.197. Parameters of open loop steering test

Figure 18.198. Speed difference $\Delta V$ versus time
18.2.4.5.6.3. Test with driver

In addition to the standard parameters for test with longitudinal motion of TV, Sect. 18.2.4.5.6. "Tests with longitudinal motion of TV", p. 18-160, the test requires the following data, Figure 18.199:

- **type of turning mechanism**, Sect. 18.2.2.1. "General information about controlled motion of TV", p. 18-119,
- **Macrogeometry type**
  - **2D curve**, Sect. 18.2.2.3.2. "Plane curve", p. 18-121, a file with a path curve must be assigned;
  - **3D testing area**, Sect. 18.2.2.3.3. "Testing area", p. 18-122, 18.2.4.1.3.1. "Testing area", p. 18-130, a testing area must be loaded; if necessary, a list of routes is created (Sect. 18.2.4.1.3.1. "Testing area", p. 18-130); after that a current route should be assigned from the drop-down list, Figure 18.199.
To set the plot of TV speed along the route, the button is used. After the click on this button, the program opens the tab for setting speed history, Sect. 18.2.4.3. "Tools tab: setting speed history", p. 18-136. A plot template containing all the route markers is created automatically. All markers are shifted backwards on the TV length. The user should edit the plot in the curve editor, Figure 18.200, save data in a file and assign this file on the test parameter tab, the Speed history group, Figure 18.199.
18.2.5. Solver

The **Park parallel** solver is used for simulation of TV dynamics. This method is developed by authors of UM in 2009 specially for simulation of large models, in particular, with multi-core processors.

Parameters of the solver are set on the corresponding tab of the inspector. Typical parameter values are shown in Figure 18.201. The following remarks are important.

- The **Use threads** key can be used for **multi-core processors only**.
- The **Number of threads** parameter must not exceed the number of physical and logical cores on the local computer, which is specified automatically. It is recommended to test different values of this parameter to choose the optimal number of threads.
- The **CG error** parameter (parameter of accuracy of the conjugate gradient method) is selected by the user after a number of tests. The optimal value of this parameter corresponds to the fastest simulation.

![Object simulation inspector](image)

Figure 18.201. Recommended solver parameters
18.2.6. List of special variables for tracked vehicles

Analysis of TV dynamics is based on computation of dependences of some variables on time. Most of the variables are created with the Wizard of variables. To call the wizard, the Tools | Wizard of variables... menu command or the button are used. Getting standard variables with the wizard is described in Chapter 4, Sect. Wizard of variables, List of variables.

![Image of wizard of variables]

Figure 18.202. List of special TV variables

Here we consider variables related to the dynamics of TV only, the Tracked vehicle tab of the wizard, Figure 18.202, Table 18.23.

<table>
<thead>
<tr>
<th>Name of variable</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>VSprocket</td>
<td>(m/s) Circular velocity of sprocket ( v = \omega R_s ), where ( \omega R_s ) are the angular velocity of the sprocket and the radius on pin centers.</td>
</tr>
<tr>
<td>MSprocket</td>
<td>(Nm) Drive torque by control of TV speed.</td>
</tr>
<tr>
<td>FTrack</td>
<td>(N) Mean track tension, ( S = \frac{\sum_{i=1}^{n} S_i}{n} ) where ( S_i ) is the force in the joint for track link ( i ), ( n ) is the number of links.</td>
</tr>
<tr>
<td>Variable</td>
<td>Description</td>
</tr>
<tr>
<td>-------------------</td>
<td>-----------------------------------------------------------------------------</td>
</tr>
<tr>
<td>NGround</td>
<td>(N) Normal force applied to a link from the ground. Number of variables is equal to the number of links.</td>
</tr>
<tr>
<td>FFrGroundX</td>
<td>(N) Friction force applied to a link from the ground in longitudinal direction. Number of variables is equal to the number of links.</td>
</tr>
<tr>
<td>FFrGroundY</td>
<td>(N) Friction force applied to a link from the ground in lateral direction. Number of variables is equal to the number of links.</td>
</tr>
<tr>
<td>RTrackLink</td>
<td>(N) Longitudinal force in a link joint Si. Number of variables is equal to the number of links.</td>
</tr>
<tr>
<td>FSprocket</td>
<td>(N) Magnitude of a pin'sprocket force. Number of variables is equal to the number of links.</td>
</tr>
<tr>
<td>NRWheel</td>
<td>(N) Road wheel loads. Number of variables is equal to the number of road wheels.</td>
</tr>
<tr>
<td>Distance</td>
<td>(м) Distance from the motion start. The variable is used in the main tests.</td>
</tr>
</tbody>
</table>

Figure 18.203. Histogram window

**Remark.** A histogram window is useful for analysis of large number of variables, Figure 18.203.
18.2.7. Features of multivariant calculations with TV

Consider some features of analysis of a TV dynamics with *UM Experiments* module.

18.2.7.1. Use of standard internal identifiers

Standard internal identifiers are introduced for some parameters specified by the user to increase the efficiency of the UM Experiments module in analysis of TV. These identifiers are used for variation of the corresponding parameters in the set of numeric experiments.

![Figure 18.204. Use of standard internal identifiers](image)

The list of standard internal identifiers is available in the parameter tree on the tab `Alternatives | Hierarchy of parameters | List of parameters`, branch `TVParameters`, Figure 18.204.

The standard internal identifier `_preload_tension` is used in the example in Figure 18.204 for planning of three computations with different stiffness constant in a flexible joint parameterized in the TV model by the usual identifier `cx`. The standard internal identifier is used for simultaneous modification of the bushing preload, which set the desired track tension for different values of bushing stiffness.
Test: tension by preload, as well as Figure 18.154). Three numeric experiments will be run according to the plan:

variant 1: cx=67 700 000 N/m, _preload_tension=35 kN,
variant 2: cx=90 252 000 N/m, _preload_tension=38 kN,
variant 3: cx=112 800 000 N/m, _preload_tension=41.5 kN.

The full list of standard internal identifiers is available in Table 18.24.

<table>
<thead>
<tr>
<th>Branch of the parameter tree</th>
<th>Name of identifier</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>General</td>
<td>_irr_type</td>
<td>Type of irregularities: 1 – file, 2 – sinusoidal, Sect. 18.2.4.1.2. &quot;Irregularities&quot;, p. 18-126, Figure 18.155</td>
</tr>
<tr>
<td></td>
<td>_dl_tension</td>
<td>(mm) Elongation of tension rod, Sect. 18.2.4.1.1. &quot;General options&quot;, p. 18-125, Figure 18.154</td>
</tr>
<tr>
<td></td>
<td>_preload_tension</td>
<td>(kN) Joint (bushing) preload, Sect. 18.2.4.1.1. &quot;General options&quot;, p. 18-125, Figure 18.154</td>
</tr>
<tr>
<td>Harmonic irregularities</td>
<td>_a</td>
<td>(m) Amplitude</td>
</tr>
<tr>
<td>Sect. 18.2.4.1.2.2. &quot;Harmonic irregularities&quot;, p. 18-127, Figure 18.155.</td>
<td>_l</td>
<td>(m) Wave length</td>
</tr>
<tr>
<td></td>
<td>_x0</td>
<td>(m) Phase shift of left wave</td>
</tr>
<tr>
<td>Track contact parameters</td>
<td>_c_ground</td>
<td>Ground stiffness (N/m)</td>
</tr>
<tr>
<td>Sect. 18.2.4.4.1. &quot;Track contact parameters&quot;, p. 18-138.</td>
<td>_beta_ground</td>
<td>Ground damping ratio</td>
</tr>
<tr>
<td></td>
<td>_ffr_ground</td>
<td>Coefficient of ground friction</td>
</tr>
<tr>
<td></td>
<td>_c_sprocket</td>
<td>Sprocket stiffness (N/m)</td>
</tr>
<tr>
<td></td>
<td>_beta_sprocket</td>
<td>Sprocket damping ratio</td>
</tr>
<tr>
<td></td>
<td>_ffr_sprocket</td>
<td>Coefficient of sprocket friction</td>
</tr>
<tr>
<td></td>
<td>_c_roadwheel</td>
<td>Road wheel stiffness (N/m)</td>
</tr>
<tr>
<td></td>
<td>_beta_roadwheel</td>
<td>Road wheel damping ratio</td>
</tr>
<tr>
<td></td>
<td>_ffr_wheel</td>
<td>Coefficient of wheel friction</td>
</tr>
<tr>
<td></td>
<td>_c_idler</td>
<td>Idler stiffness (N/m)</td>
</tr>
<tr>
<td></td>
<td>_beta_idler</td>
<td>Idler damping ratio</td>
</tr>
<tr>
<td></td>
<td>_c_roller</td>
<td>Roller stiffness (N/m)</td>
</tr>
<tr>
<td></td>
<td>_beta_roller</td>
<td>Roller damping ratio</td>
</tr>
<tr>
<td></td>
<td>_c_lateral</td>
<td>Lateral stiffness (N/m)</td>
</tr>
<tr>
<td></td>
<td>_beta_lateral</td>
<td>Lateral damping ratio</td>
</tr>
<tr>
<td></td>
<td>_h_guidetooth</td>
<td>Guide tooth height (mm)</td>
</tr>
</tbody>
</table>
Let us consider an example of a multivariant experiment in which a TV moves on different sinusoidal irregularities with different speed values, Figure 18.205.

![Graph](image)

**Figure 18.205. Plan of multivariant calculations**

In this example, the plan includes 15 computations for five speeds (10, 20, 30, 40, 50 km/h). Three computations with different sinusoidal irregularities are planned for each of the speed values:

- **Variant 1**: amplitude 3 cm, length 5 m;
- **Variant 2**: amplitude 4 cm, length 7 m;
- **Variant 3**: amplitude 5 cm, length 9 m.

### 18.2.7.2. Finish conditions of experiments by distance

It is useful to set the finish conditions by distance from the start for computation of motion with different speeds. As a result, the distance will be the same for all the experiments. The following steps are to be made to assign the corresponding finish condition.
Create the distance variable, Figure 18.206.

Drag the variable into the box on the Alternatives | Finish conditions tab, Figure 18.207.

Set the distance value (100 m in Figure 18.207).
18.3. References